

Napoli, 15 October '04

## Concluding Talk

G. Altarelli

CERN

Not a "Summary": too many talks, too few days  
also I am not competent on many technical aspects.

Not a "Conclusion": a gigantic work in progress.

Rather a status of the physics LHC is going to address

Overall the EW precision tests support the SM and a light Higgs.

The  $\chi^2$  is reasonable:

$\chi^2/\text{ndof} \sim 16/13$  ( $\sim 23\%$ )

Note: does not include NuTeV, APV, Moeller and  $(g-2)_\mu$

Recent!!  $\longrightarrow$

New!!  $\longrightarrow$

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Winter 2004



# Low Energy Experiments

~3σ away!?

NuTeV  
APV  
Moeller

Observable	Measurement	SM fit
$\sin^2 \theta_W$ ( $\nu N$ [10])	$0.2277 \pm 0.0016$	0.2226
$Q_W(\text{Cs})$ (APV [11])	$-72.84 \pm 0.49$	-72.91
$\sin^2 \theta_{\text{eff}}^{\text{lept}}$ ( $e^- e^-$ [12])	$0.2296 \pm 0.0023$	0.2314

New!!

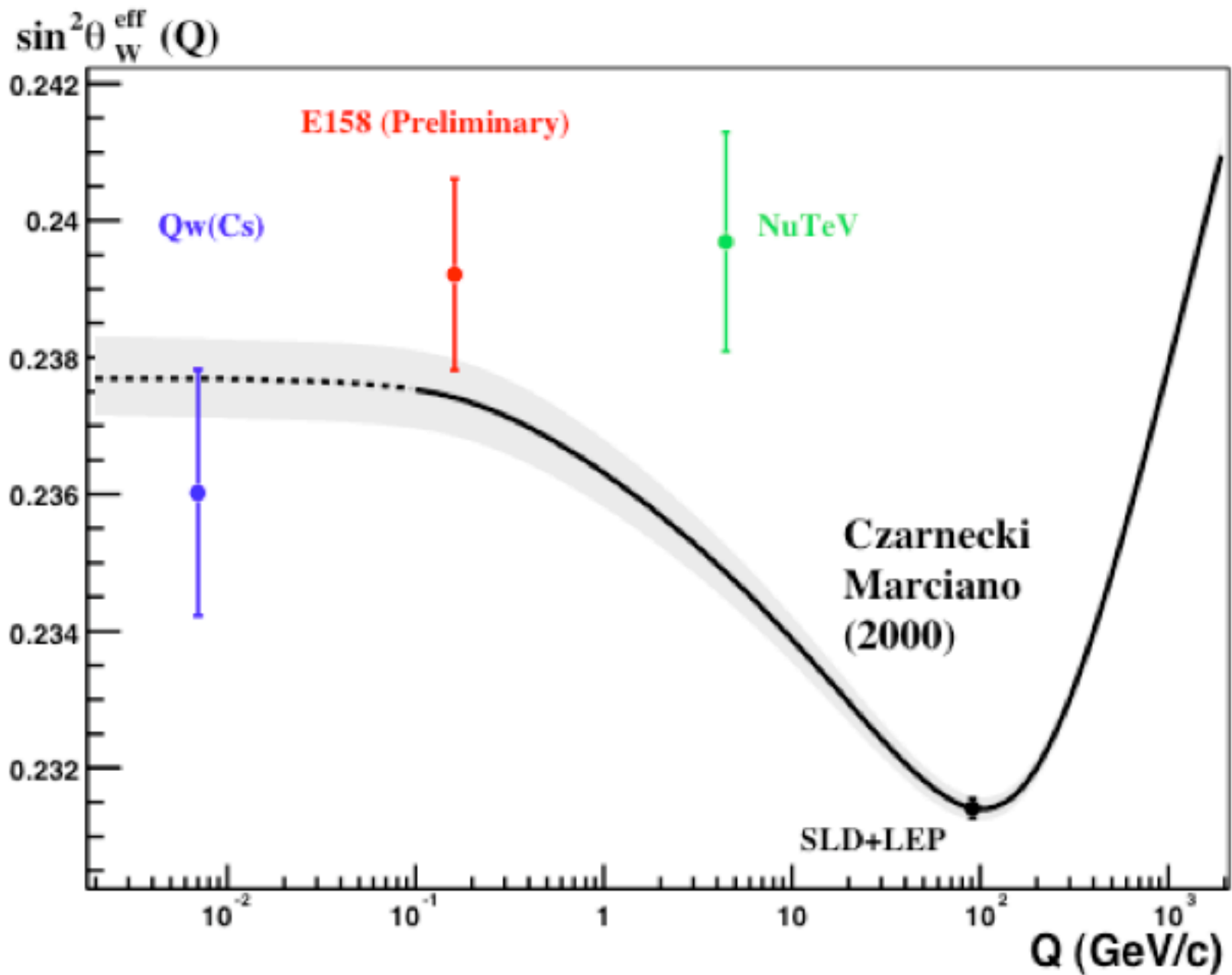
$$A_{PV} = \frac{(\sigma_R - \sigma_L)}{(\sigma_R + \sigma_L)}$$

ICHEP'04:  $0.2330 \pm 0.0015$

recall for comparison:  
present WA  
 $\sin^2 \theta_{\text{eff}} = 0.23148 \pm 0.00017$

(g-2) not included here  
[no  $m_H$  implications]

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G

The NuTeV anomaly probably simply arises from a large underestimation of the theoretical error

- The QCD LO parton analysis is too crude to match the required accuracy
- A small asymmetry in the momentum carried by s-sbar could have a large effect

They claim to have measured this asymmetry from dimuons. But a LO analysis of s-sbar makes no sense and cannot be directly transplanted here ( $\alpha_s$ \*valence corrections are large and process dependent)

- A tiny violation of isospin symmetry in parton distrib's can also be important.

S. Davidson, S. Forte, P. Gambino, N. Rius, A. Strumia

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# $(g-2)_\mu \sim 3\sigma$ discrepancy shown by the BNL'02 data

In 2002:

(Numbers in units  $10^{-10}$ )

LO hadr.	$688.8 \pm 6.2$	HMNT, 'excl.'
	$683.1 \pm 5.9 \pm 2.0_{rad}$	HMNT, 'incl.'
full $a_\mu$	$11659172.6 \pm 7.7$	'excl.'
	$11659166.9 \pm 7.4$	'incl.'
BNL E821	$11659203 \pm 8$	new world av.
		(0.7 ppm!)
EXP-TH	$30.4 \pm 11.1$	$\sim 2.7\sigma$ , 'excl.'
	$36.1 \pm 10.9$	$\sim 3.3\sigma$ , 'incl.'

Th. and Exp. accuracy comparable!

EW  $\sim 15.2 \pm 0.4$

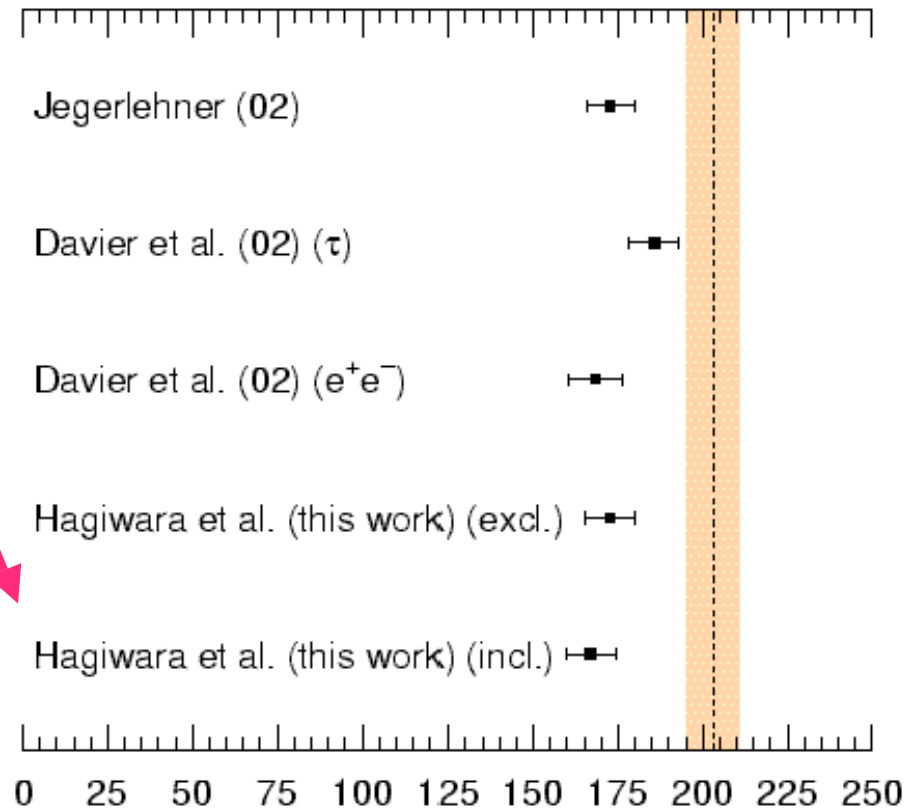
LO hadr  $\sim 683.1 \pm 6.2$

NLO hadr  $\sim -10 \pm 0.6$

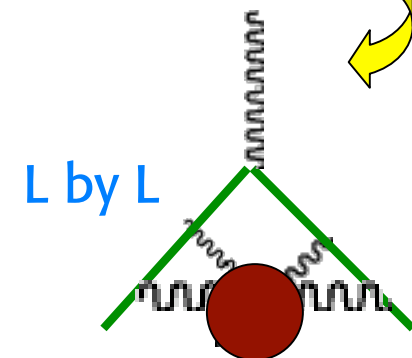
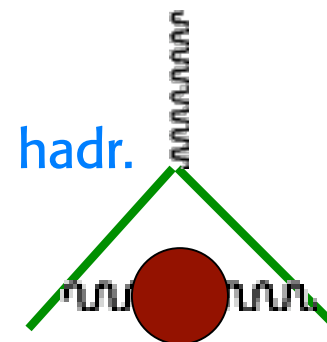
Light-by-Light  $\sim 8 \pm 4$

(was  $\sim -8.5 \pm 2.5$ )

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These units



The discrepancy is less: 2-2.5  $\sigma$

2003

(new measurements of  $\sigma_{had}$ )

# The spectral function from $e^+e^-$

Tau data below 1.8 GeV

Final CMD-2  $\pi\pi$  data (2002) 0.6% syst error!  
 CMD-2 have recently reanalyzed their data

Hagiwara et al (HMNT) NEW result:

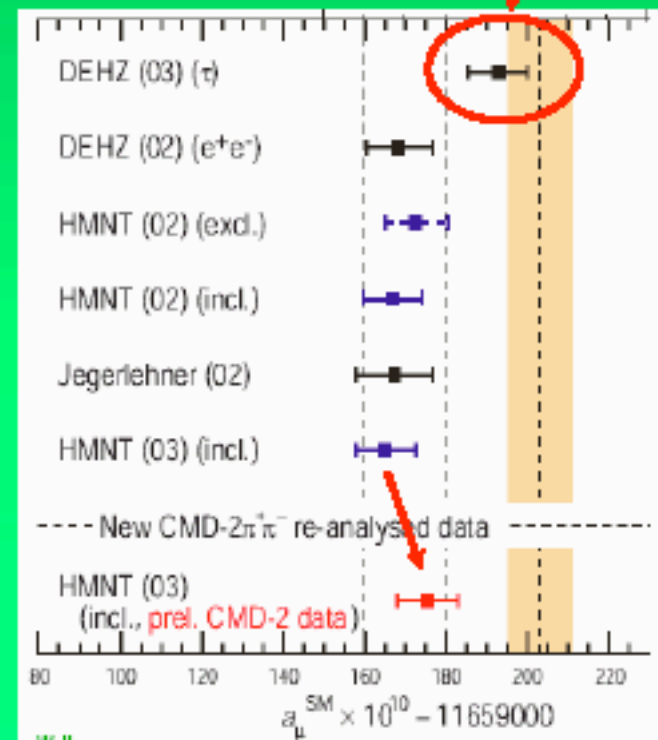
$$a_{\mu}^{had,LO} = 691.7 \pm 5.8_{exp} \pm 2.0_{r.c.}$$

This translates in a  $\sim 2-2.5\sigma$  discrepancy depending on which  $e^+e^-$  analysis

Using  $\tau$  data below 1.8 GeV Davier et al (DEHZ)

$$a_{\mu}^{had,LO} = 709.0 \pm 5.1_{exp} \pm 1.2_{r.c} \pm 2.8_{SU(2)}$$

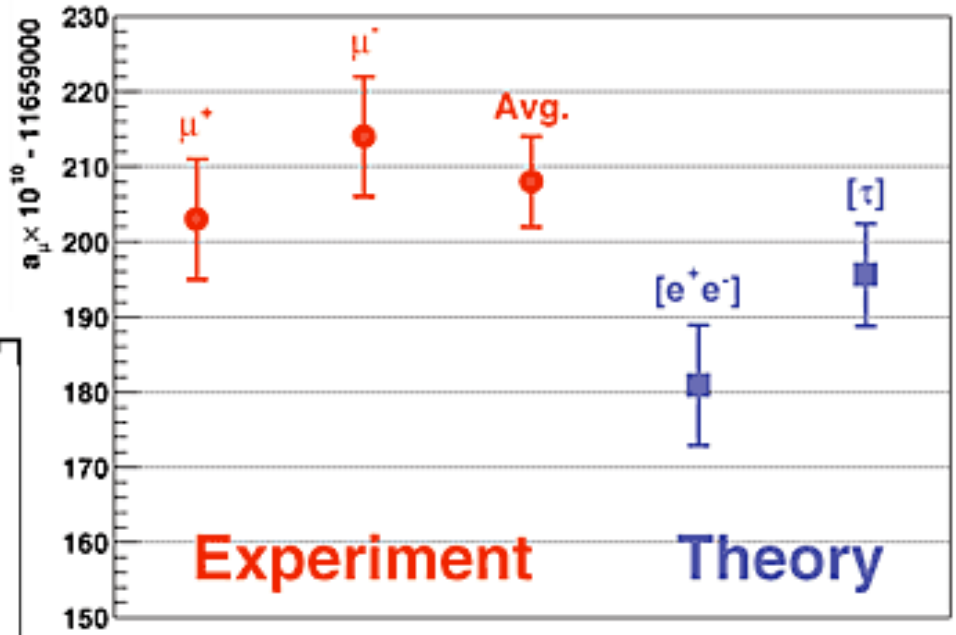
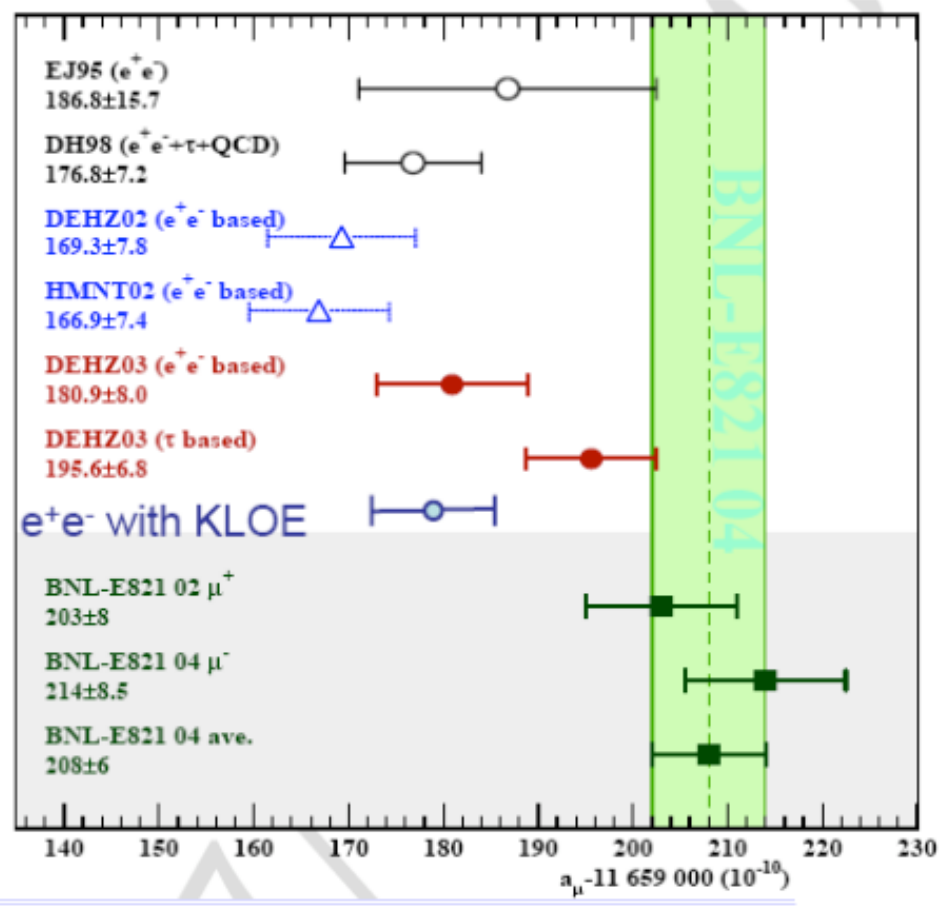
Good agreement between Aleph, CLEO, Opal  $\tau$  data



The  $\tau$  data indicate no discrepancy!

# 2004 **New** New results from BNL

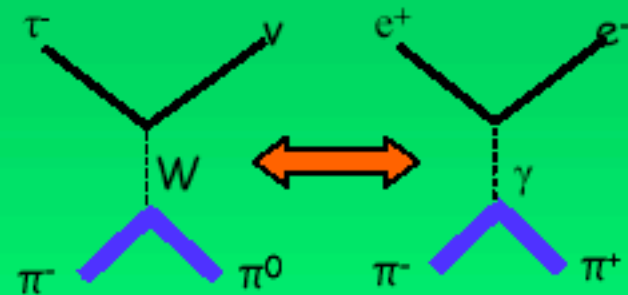
- $\mu^-$  measured (was  $\mu^+$ )
- discrepancy up again to  $2.7\sigma$  ( $e^+e^-$ )



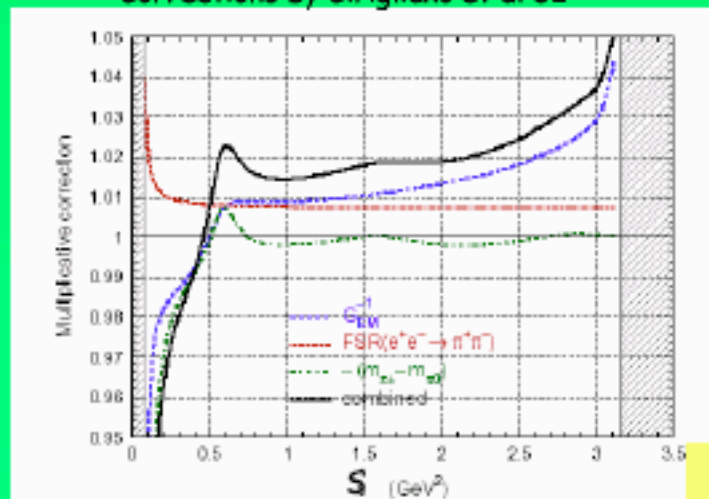
ICHEP'04



# The spectral function from $\tau$ decays

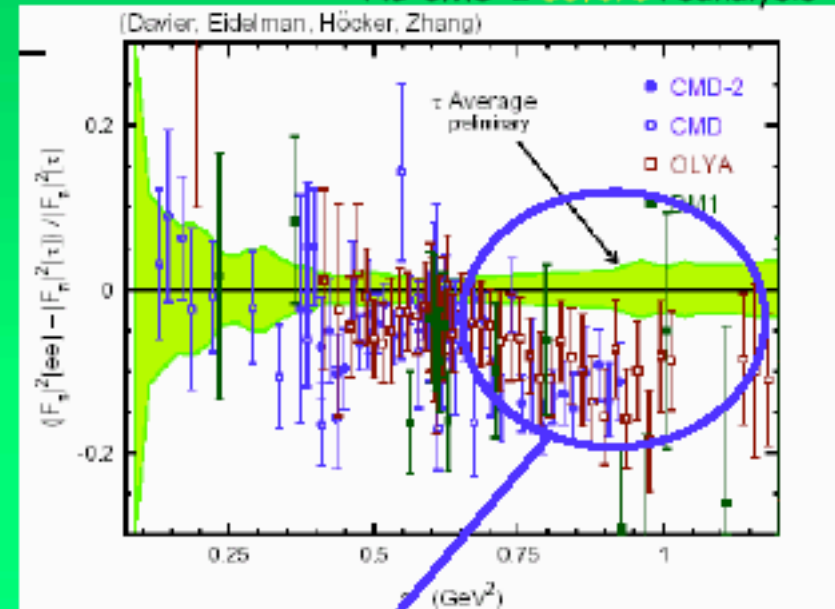


CVC + isospin symmetry  
 Corrections by Cirigliano et al 02



Corrections applied to  $\tau$  data

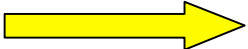
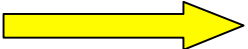
NB CMD-2 before reanalysis



Relative difference between  $\pi$  form f. from  $\tau$  and  $e^+e^-$

>5% difference! cannot be isospin breaking. Needs further study. Data?  
 After new CMD-2 for  $\Delta_{\pi\pi} = (11-13 \pm 7) \cdot 10^{-10}$  (was 21)

## Question Marks on EW Precision Tests

- The measured values of  $\sin^2\theta_{\text{eff}}$  from leptonic ( $A_{\text{LR}}$ ) and from hadronic ( $A_{\text{FB}}^b$ ) asymmetries are  $\sim 3\sigma$  away 
- The measured value of  $m_W$  is a bit high   
(now better because  $m_t$  went up)
- The central value of  $m_H$  ( $m_H = 113+62-42$  GeV) from the fit is at the direct lower limit ( $m_H < 114.4$  GeV at 95%)  
[more so if  $\sin^2\theta_{\text{eff}}$  is close to that from leptonic ( $A_{\text{LR}}$ ) asymm.  
 $m_H = 70+49-31$  GeV] (also much better now)

Used to be an issue:

2001: Chanowitz;

GA, F. Caravaglios, G. Giudice, P. Gambino, G. Ridolfi

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# Status of $\sin^2\theta_{\text{eff}}$

Combined lept. asymm.:

$$[\sin^2\theta]_{\text{lept}} = 0.23117(20)$$

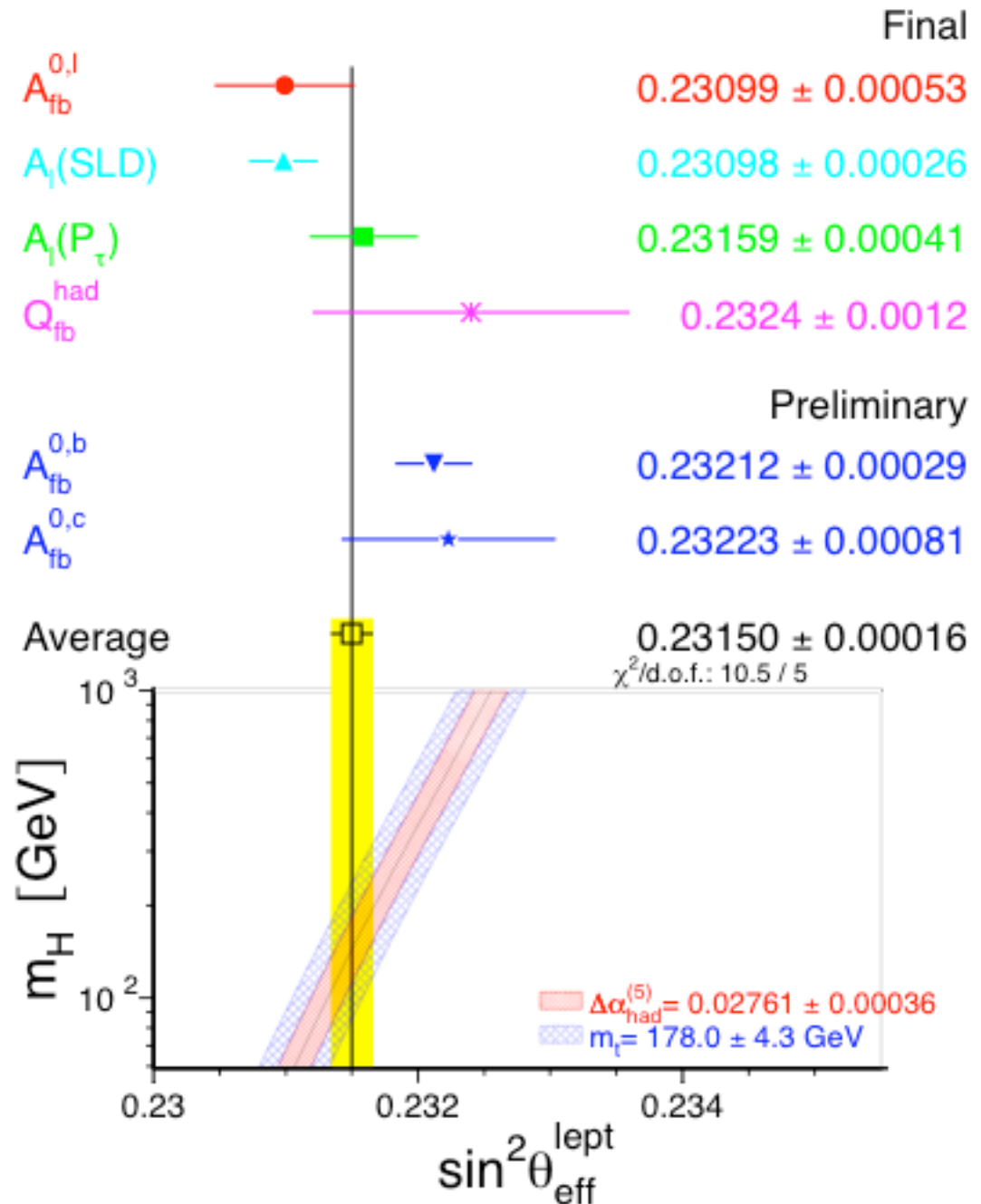
Combined hadr. asymm.:

$$[\sin^2\theta]_{\text{hadr}} = 0.23213(27)$$



diff = 2.8  $\sigma$

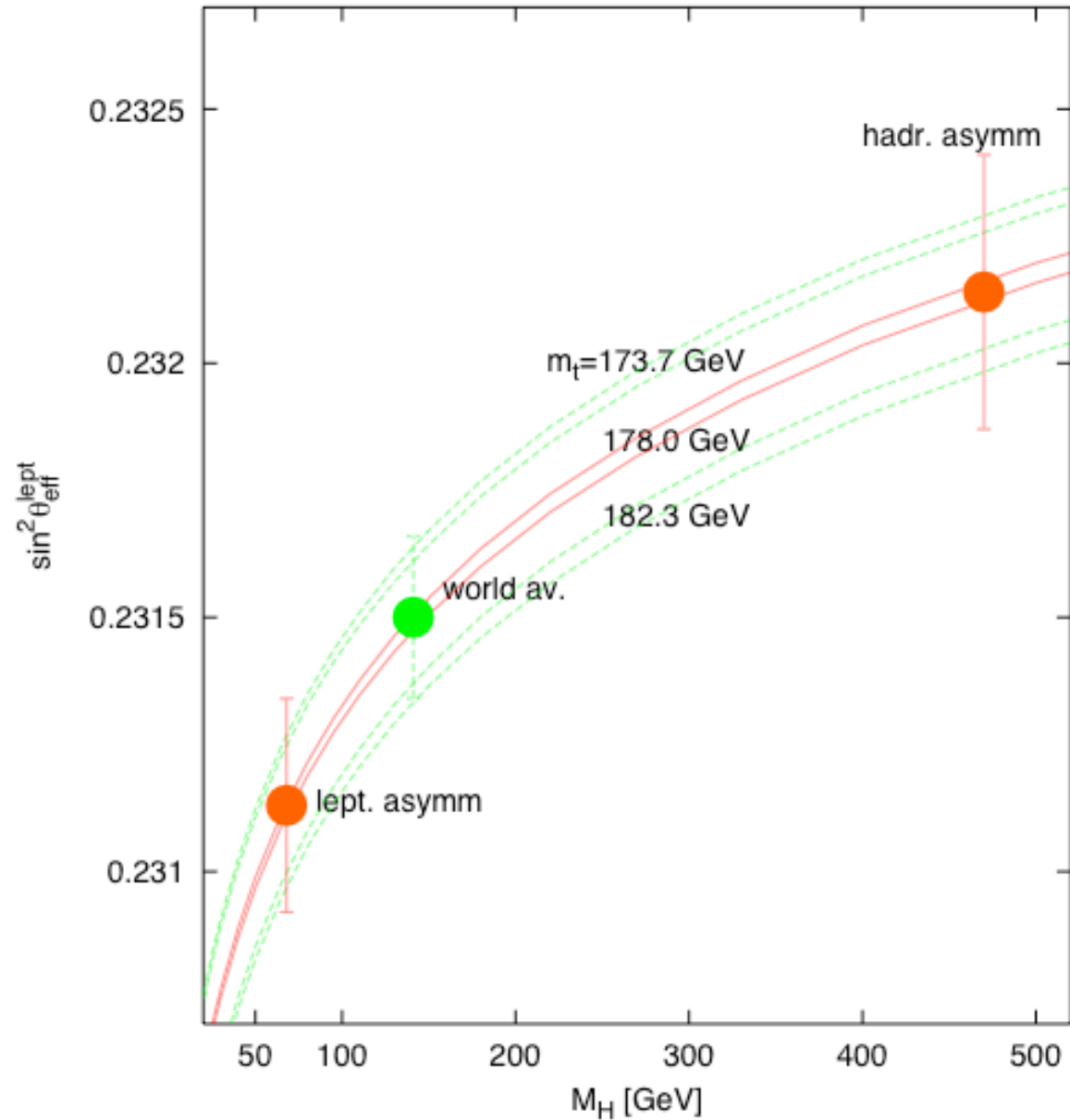
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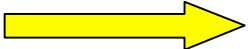
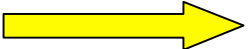
Plot  $\sin^2\theta_{\text{eff}}$  vs  $m_H$

Exp. values are plotted at the  $m_H$  point that better fits given  $m_{\text{texp}}$

Clearly leptonic and hadronic asymms. push  $m_H$  towards different values



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Plot  $m_W$  vs  $m_H$

$m_W$  points to a light Higgs

Like  $[\sin^2\theta_{\text{eff}}]_l$

Recently:

$m_W$  ↓

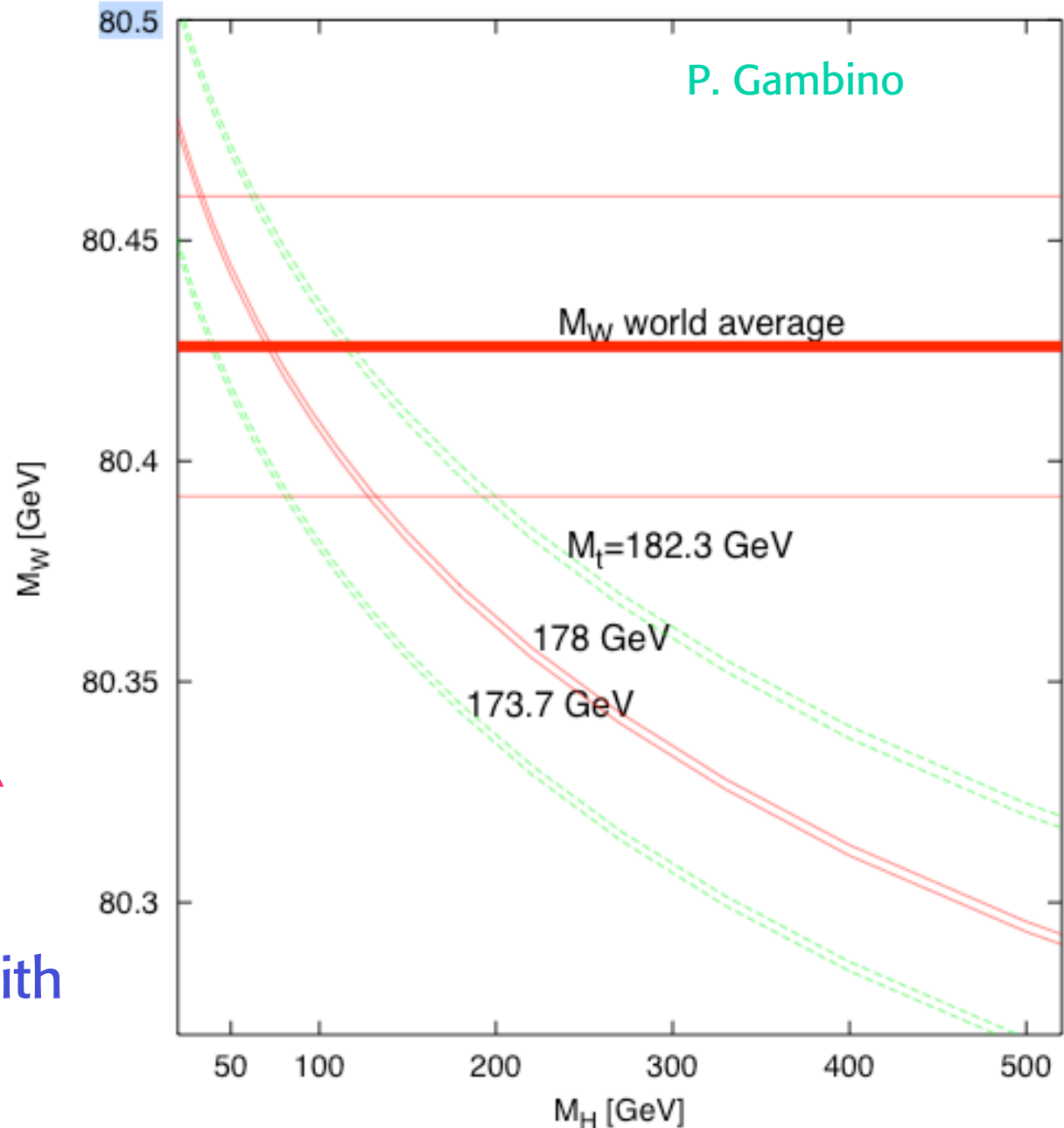
$m_t$  ↑

Aleph

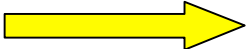
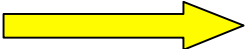
D0

Better agreement with  $m_H > 114$  GeV

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## Question Marks on EW Precision Tests

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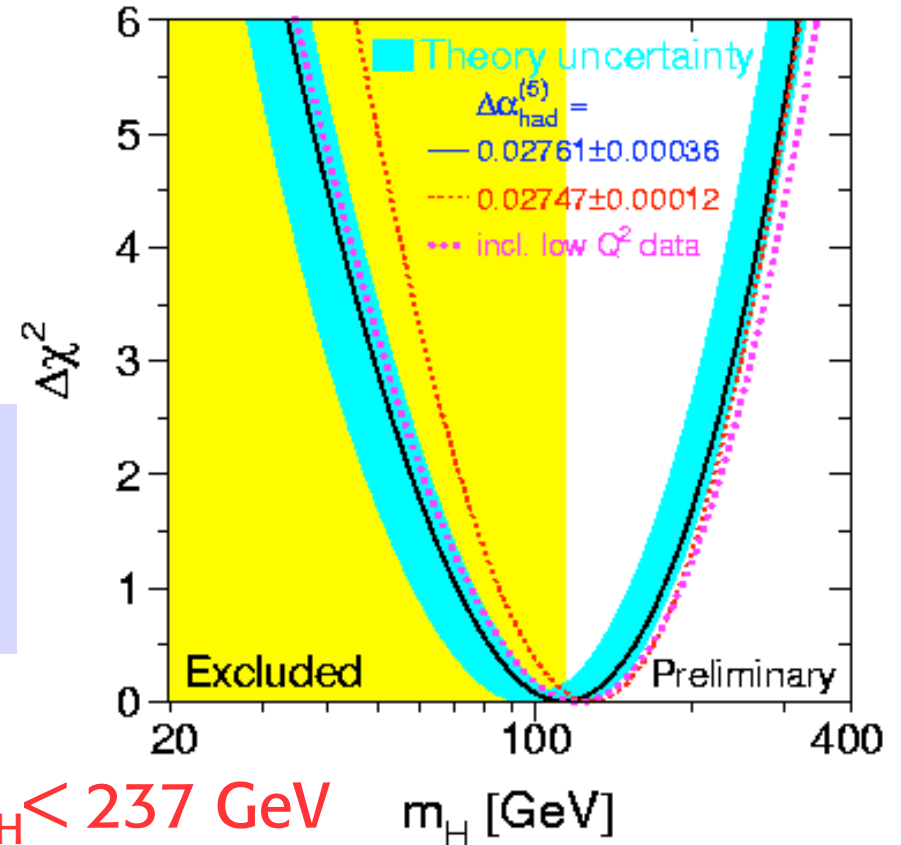
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# Status of the SM Higgs fit

Winter '04

Rad Corr.s  $\rightarrow$  Sensitive to  $\log m_H$   
 $\log_{10} m_H(\text{GeV}) = 2.05 \pm 0.20$

This is a great triumph for the SM: right in the narrow allowed window  $\log_{10} m_H \sim 2 - 3$



Direct search:  $m_H > 114 \text{ GeV}$

$m_H < 237 \text{ GeV}$

G. A

Measurements	$m_W, \Gamma_W$	$m_t$	$m_t, m_W, \Gamma_W$
$m_t$ (GeV)	$178.5^{+11.0}_{-8.5}$	$177.2 \pm 4.1$	$178.1 \pm 3.9$
$m_H$ (GeV)	$117^{+162}_{-62}$	$129^{+76}_{-50}$	$113^{+62}_{-42}$
$\log [m_H(\text{GeV})]$	$2.07^{+0.38}_{-0.33}$	$2.11 \pm 0.21$	$2.05 \pm 0.20$
$\alpha_s(m_Z)$	$0.1187 \pm 0.0027$	$0.1190 \pm 0.0027$	$0.1186 \pm 0.0027$
$\chi^2/dof$	16.3/12	15.0/11	16.3/13



$\log_{10} m_H \sim 2$  is a very important result

Drop H from SM  $\rightarrow$  renorm. lost  $\rightarrow$  divergences  $\rightarrow$  cut-off  $\Lambda$

$$\log m_H \rightarrow \log \Lambda + \text{const}$$

Any alternative mechanism amounts to change the prediction of finite terms.

The most sensitive quantities to  $\log m_H$  are  $\varepsilon_1 \sim \Delta\rho$  and  $\varepsilon_3$ :

$\log_{10} m_H \sim 2$  means that  $f_{1,3}$  are compatible with the SM prediction

$$\varepsilon_1 = - \underbrace{\frac{3 G_F m_W^2}{4\pi^2 \sqrt{2}} \text{tg}^2 \theta_W}_{-1.2 \cdot 10^{-3}} \left[ \log \frac{m_H}{m_Z} + f_1 \right]$$

New physics can change the bound on  $m_H$  (different  $f_{1,2}$ )

$$\varepsilon_3 = \underbrace{\frac{G_F m_W^2}{12\pi^2 \sqrt{2}}}_{0.45 \cdot 10^{-3}} \left[ \log \frac{m_H}{m_Z} + f_3 \right]$$

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- It is not simple to explain the difference  $[\sin^2\theta]_l$  vs  $[\sin^2\theta]_h$  in terms of new physics.

A modification of the  $Z \rightarrow b\bar{b}$  vertex (but  $R_b$  and  $A_b$  (SLD) look  $\sim$  normal)?

- Probably it arises from an experimental problem
- Then it is very unfortunate because  $[\sin^2\theta]_l$  vs  $[\sin^2\theta]_h$  makes the interpretation of precision tests ambiguous

Choose  $[\sin^2\theta]_h$ : bad  $\chi^2$  (clashes with  $m_W$ , ...)

Choose  $[\sin^2\theta]_l$ : good  $\chi^2$ , but  $m_H$  below direct limit

- In the last case, SUSY effects from light  $s$ -leptons, charginos and neutralinos, with moderately large  $\tan\beta$  can solve the  $m_H$  problem and lead to a better fit of the data

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GA, F. Caravaglios, G. Giudice, P. Gambino, G. Ridolfi  
(updated 2004)

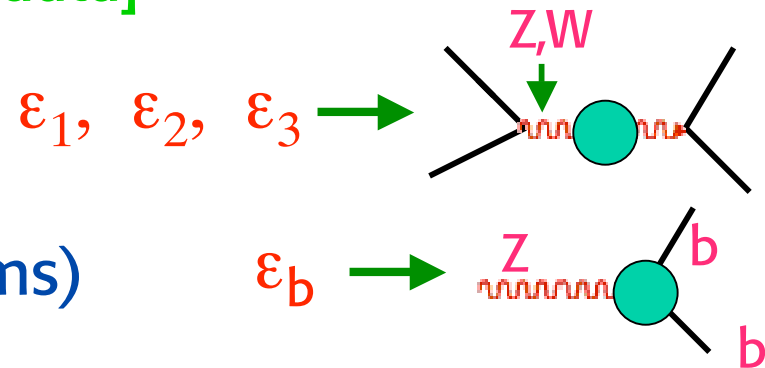
## EW DATA and New Physics

For an analysis of the data beyond the SM we use the  $\epsilon$  formalism GA, R.Barbieri, F.Caravaglios, S. Jadach

One introduces  $\epsilon_1, \epsilon_2, \epsilon_3, \epsilon_b$  such that:

- Focus on pure weak rad. correct's, i.e. vanish in limit of tree level SM + pure QED and/or QCD correct's [a good first approximation to the data]

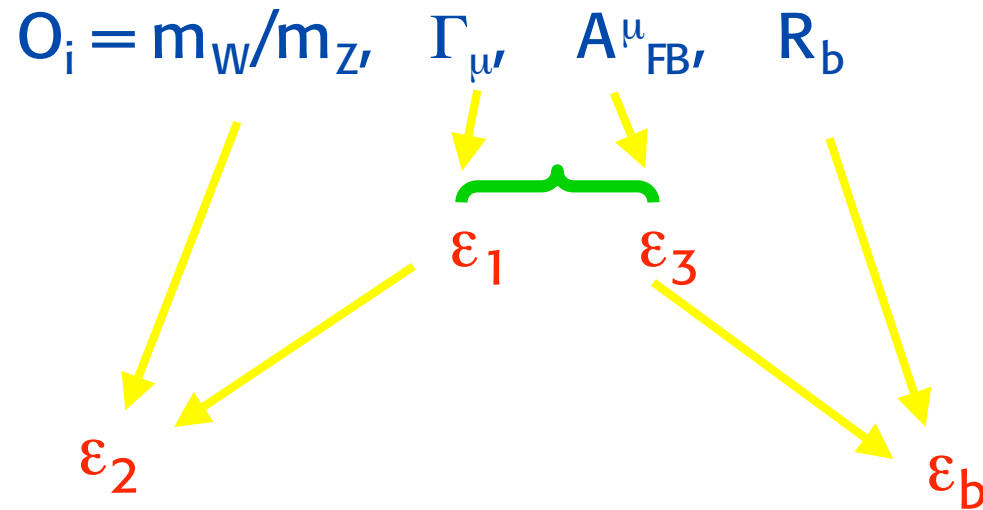
- Are sensitive to vacuum pol. and Z- $\rightarrow$ bb vertex corr.s (but also include non oblique terms)



- Can be measured from the data with no reference to  $m_t$  and  $m_H$  (as opposed to S, T, U  $\rightarrow \epsilon_3, \epsilon_1, \epsilon_2$ )

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One starts from a set of defining observables:



$$O_i[\varepsilon_k] = O_i^{\text{"Born"}}[1 + A_{ik} \varepsilon_k + \dots]$$

$O_i^{\text{"Born"}}$  includes pure QED and/or QCD corr's.

$A_{ik}$  is independent of  $m_t$  and  $m_H$

Assuming lepton universality:  $\Gamma_\mu, A^{\mu}_{FB} \rightarrow \Gamma_l, A^l_{FB}$

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To test lepton-hadron universality one can add  $\Gamma_Z, \sigma_h, R_l$  to  $\Gamma_l$  etc.


The EWWG gives (winter '04):

$$\begin{aligned}\varepsilon_1 &= 5.4 \pm 1.0 \cdot 10^{-3} \\ \varepsilon_2 &= -8.9 \pm 1.2 \cdot 10^{-3} \\ \varepsilon_3 &= 5.25 \pm 0.95 \cdot 10^{-3} \\ \varepsilon_b &= -4.7 \pm 1.6 \cdot 10^{-3}\end{aligned}$$

Non-degenerate  
much larger shift of  $\varepsilon_1$

For comparison:

a mass **degenerate** fermion multiplet gives


$$\Delta\varepsilon_3 = N_C \frac{G_F m_W^2}{8\pi^2 \sqrt{2}} \cdot \frac{4}{3} [T_{3L} - T_{3R}]^2$$

For each member  
of the multiplet

One chiral quark doublet (either L or R):

$$\Delta\varepsilon_3 = +1.4 \cdot 10^{-3}$$

(Note that  $\varepsilon_3$  if anything is low!)

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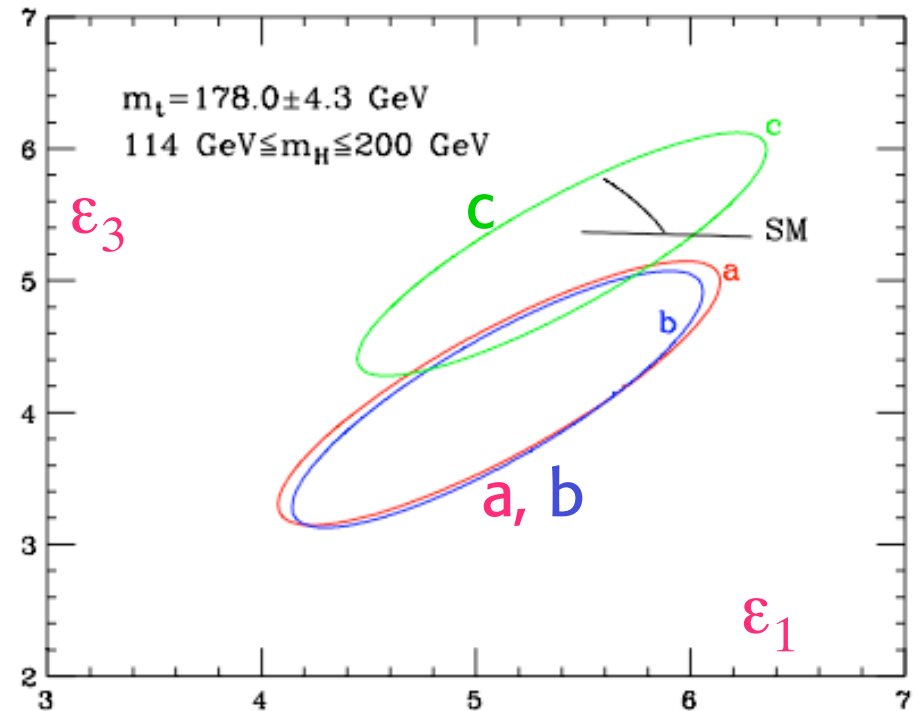
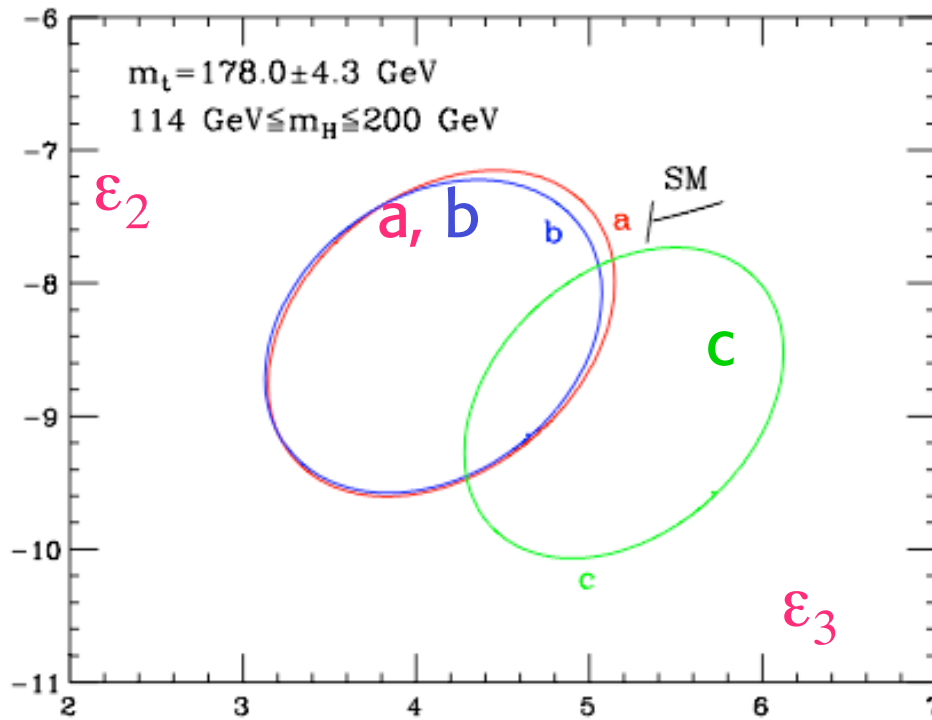
a:  $m_W, \Gamma_l, R_b, [\sin^2\theta]_l$

b:  $m_W, \Gamma_l, R_b, \Gamma_Z, \sigma_h, R_l, [\sin^2\theta]_l$

c:  $m_W, \Gamma_l, R_b, \Gamma_Z, \sigma_h, R_l, [\sin^2\theta]_l + [\sin^2\theta]_h$

Note:  
 $1\sigma$  ellipses (39% cl)

Units:  $10^{-3}$

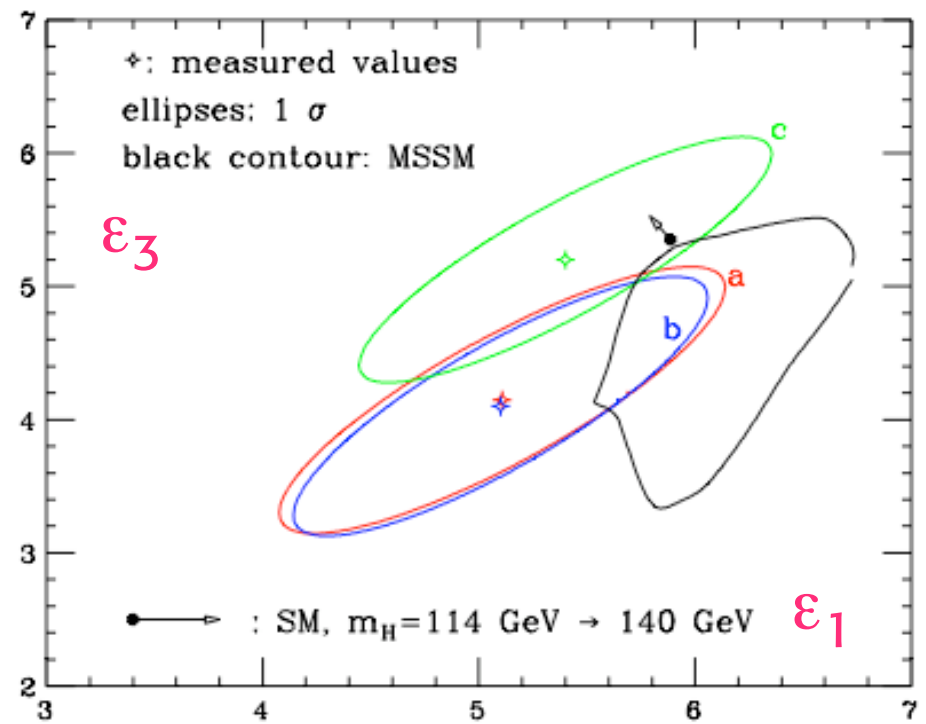
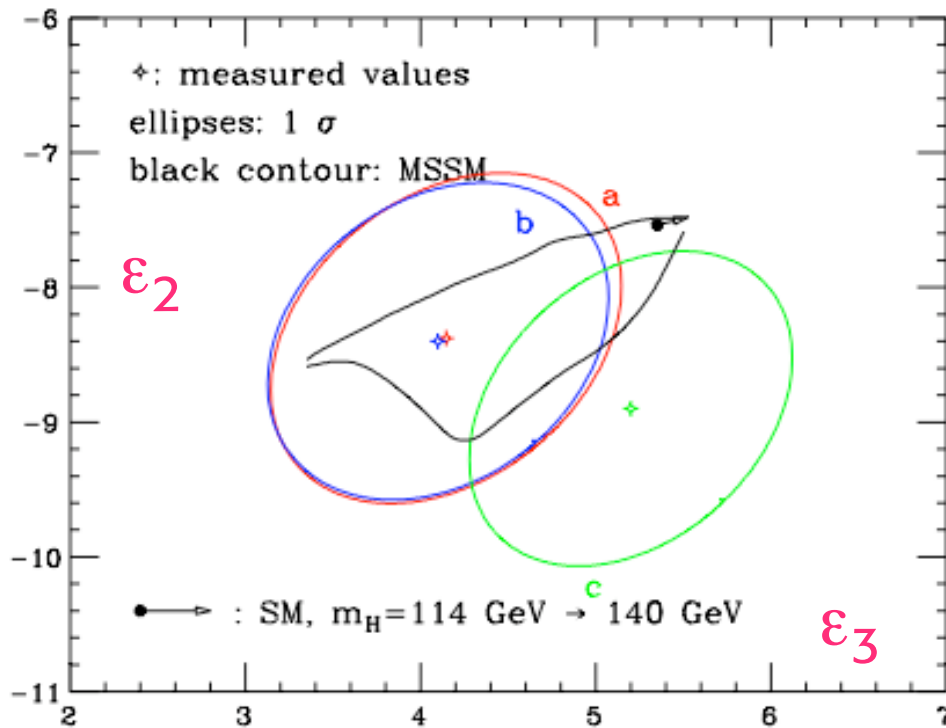


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$\epsilon_1$  is  $\sim$ OK (on the low side),  $\epsilon_2$  is a bit low ( $m_W$ ),  
 $\epsilon_3$  depends on  $\sin^2\theta$ : low for  $[\sin^2\theta]_l$  ( $m_H$ )

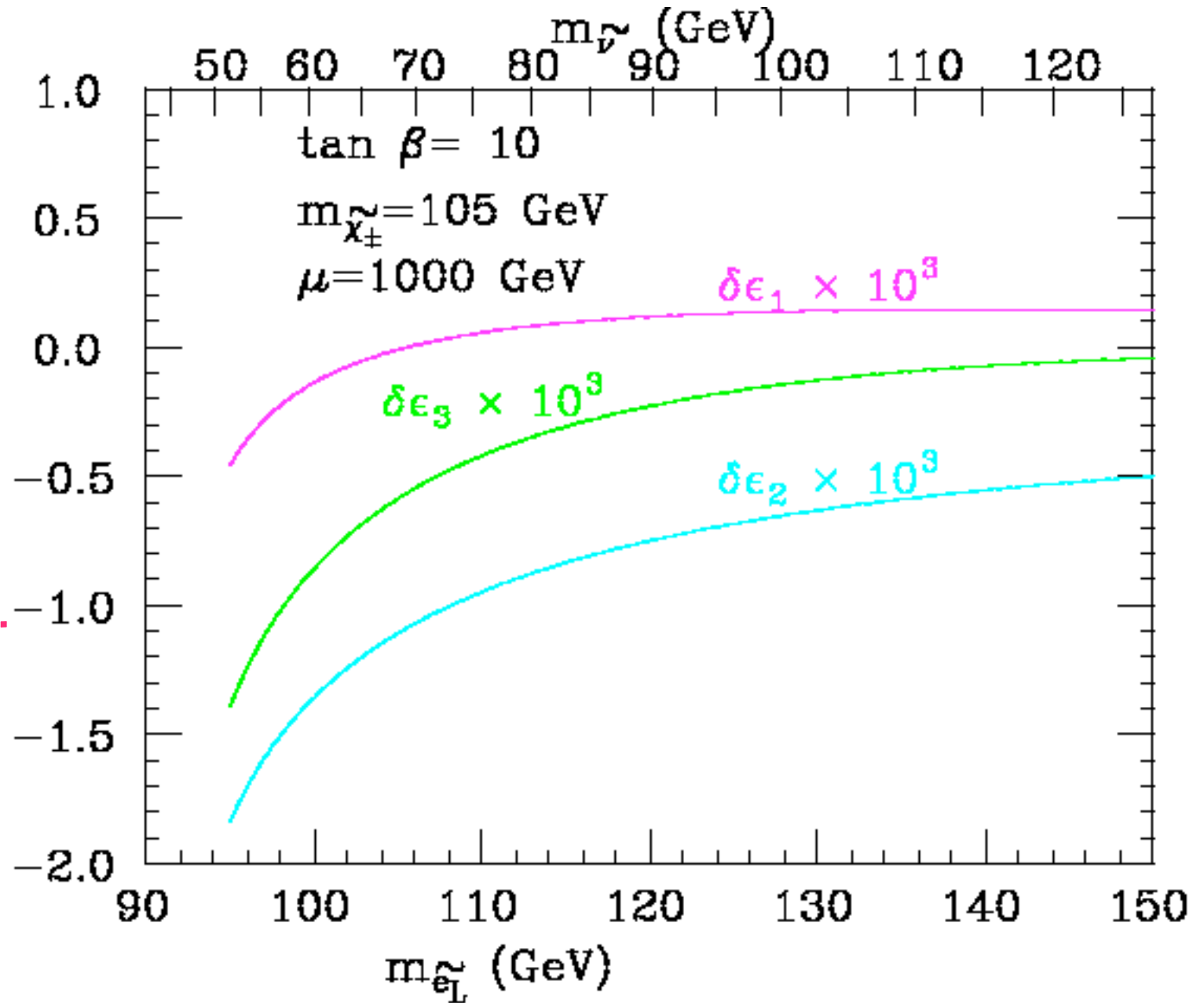
**MSSM:**  $m_{\tilde{e}_L} = 96\text{-}300$  GeV,  $m_{\chi^-} = 105\text{-}300$  GeV,  
 $\mu = (-1)\text{-}(+1)$  TeV,  $\text{tg}\beta = 10$ ,  $m_h = 114$  GeV,  
 $m_A = m_{\tilde{e}_R} = m_{\tilde{q}} = 1$  TeV

Units:  $10^{-3}$



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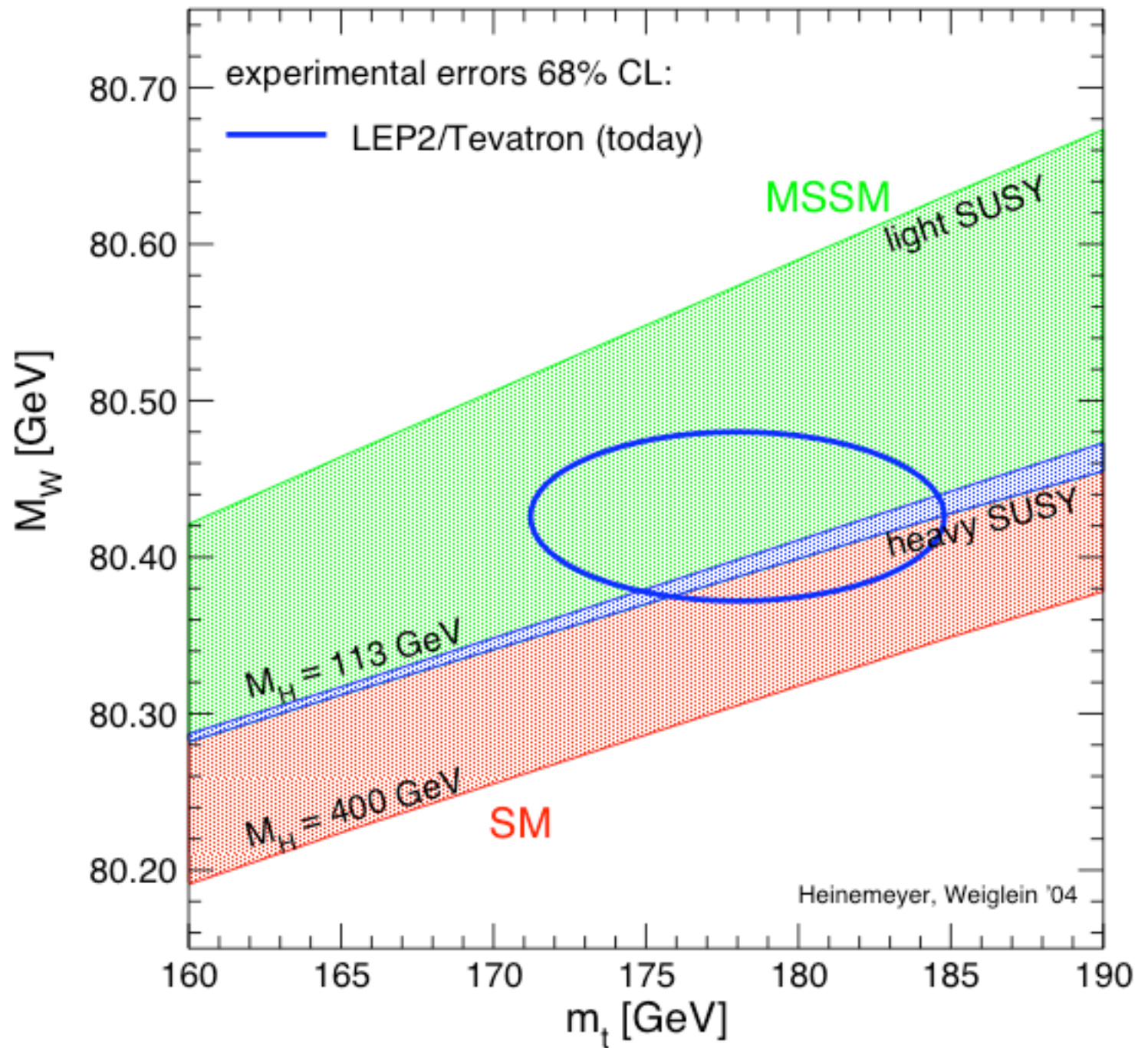
s-leptons  
and s- $\nu$ 's  
plus  
gauginos  
must be  
as light as  
possible  
given the  
present exp.  
bounds!



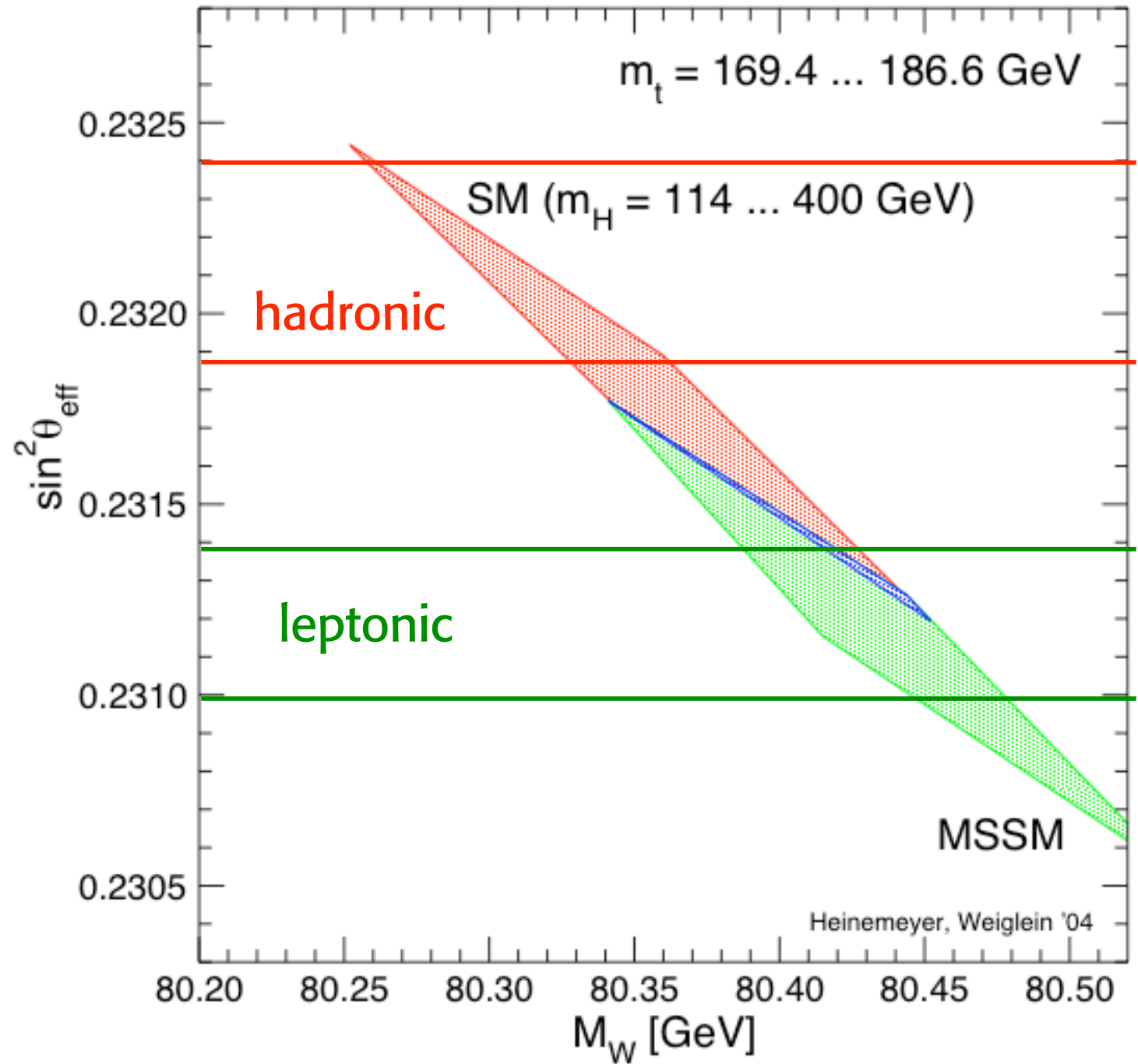
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In general in MSSM:  $m_{\tilde{e}_L}^2 = m_{\tilde{\nu}}^2 + m_W^2 |\cos 2\beta|$





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Light SUSY is compatible with  $(g-2)_\mu$

Typically at large  $\tan\beta$ :

$$\delta a_\mu \sim 150 \cdot 10^{-11} (100 \text{ GeV}/m)^2 \tan\beta$$

Exp.  $\sim 250$



OK for e.g.  $\tan\beta \sim 4$ ,  $m_{\chi^+} \sim m \sim 140 \text{ GeV}$

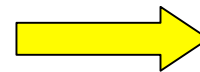
Light s-leptons and gauginos predict a deviation!

# The Standard Model works very well

So, why not find the Higgs and declare particle physics solved?

First, you have to find it!

Because of both:



LHC

## Conceptual problems

- Quantum gravity
- The hierarchy problem
- 

## and experimental clues:

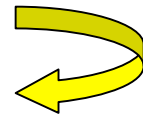
- Coupling unification
- Neutrino masses
- Baryogenesis
- Dark matter
- Vacuum energy
-

# Conceptual problems of the SM

Most clearly:

- No quantum gravity ( $M_{\text{Pl}} \sim 10^{19}$  GeV)
- But a direct extrapolation of the SM leads directly to GUT's ( $M_{\text{GUT}} \sim 10^{16}$  GeV)

$M_{\text{GUT}}$  close to  $M_{\text{Pl}}$



- suggests unification with gravity as in superstring theories
- poses the problem of the relation  $m_W$  vs  $M_{\text{GUT}} - M_{\text{Pl}}$

Can the SM be valid up to  $M_{\text{GUT}} - M_{\text{Pl}}$ ??



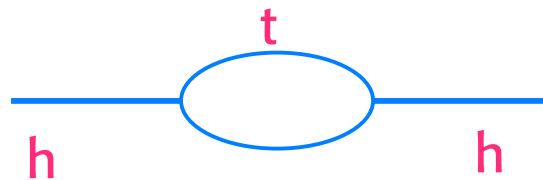
The hierarchy problem

Not only it looks very unlikely, but the new physics must be near the weak scale!

G. Altarel

For the low energy theory: the “little hierarchy” problem:

e.g. the top loop (the most pressing):



$$m_h^2 = m_{\text{bare}}^2 + \delta m_h^2$$

$$\delta m_{h|top}^2 = \frac{3G_F}{\sqrt{2}\pi^2} m_t^2 \Lambda^2 \sim (0.3\Lambda)^2$$

This hierarchy problem demands new physics near the weak scale

$\Lambda$ : scale of new physics beyond the SM

- $\Lambda \gg m_Z$ : the SM is so good at LEP
- $\Lambda \sim \text{few times } G_F^{-1/2} \sim o(1\text{TeV})$  for a natural explanation of  $m_h$  or  $m_W$

$\Lambda \sim o(1\text{TeV})$





Barbieri, Strumia

◀ **The LEP Paradox:**  $m_h$  light, new physics must be so close but its effects are not directly visible

G. Altarelli

## Examples:

- Supersymmetry: boson-fermion symm.  
exact (**unrealistic**): cancellation of  $\delta\mu^2$   
approximate (**possible**):  $\Lambda \sim m_{\text{SUSY}} - m_{\text{ord}}$   top loop  
 $\Lambda \sim m_{\text{stop}}$   
 SUSY  

The most widely accepted
- The Higgs is a  $\bar{\psi}\psi$  condensate. No fund. scalars. But needs new very strong binding force:  $\Lambda_{\text{new}} \sim 10^3 \Lambda_{\text{QCD}}$  (technicolor).  

Strongly disfavoured by LEP
- Large extra spacetime dimensions that bring  $M_{\text{Pl}}$  down to  $o(1\text{TeV})$   

Elegant and exciting. Rich potentiality. Does it work?
- Models where extra symmetries allow  $m_h$  only at 2 loops and non pert. regime starts at  $\Lambda \sim 10\text{TeV}$   

"Little Higgs" models. Technically could work

## SUSY at the Fermi scale

- Many theorists consider SUSY as established at  $M_{\text{Pl}}$  (superstring theory).
- Why not try to use it also at low energy to fix some important SM problems.
- Possible viable models exists:
  - MSSM softly broken with gravity mediation
  - or with gauge messengers
  - or with anomaly mediation
  -
- Maximally rewarding for theorists
  - Degrees of freedom identified
  - Hamiltonian specified
  - Theory formulated, finite and computable up to  $M_{\text{Pl}}$

Unique!

G. Altarelli

Fully compatible with, actually supported by GUT's



## SUSY fits with GUT's

From  $\alpha_{\text{QED}}(m_Z)$ ,  
 $\sin^2\theta_W$  measured  
at LEP predict  
 $\alpha_s(m_Z)$  for unification  
(assuming desert)

EXP:  $\alpha_s(m_Z)=0.119\pm 0.003$   
Present world average

- **Proton decay:** Far too fast without SUSY
- $M_{\text{GUT}} \sim 10^{15}\text{GeV}$  non SUSY  $\rightarrow 10^{16}\text{GeV}$  SUSY
- Dominant decay: Higgsino exchange

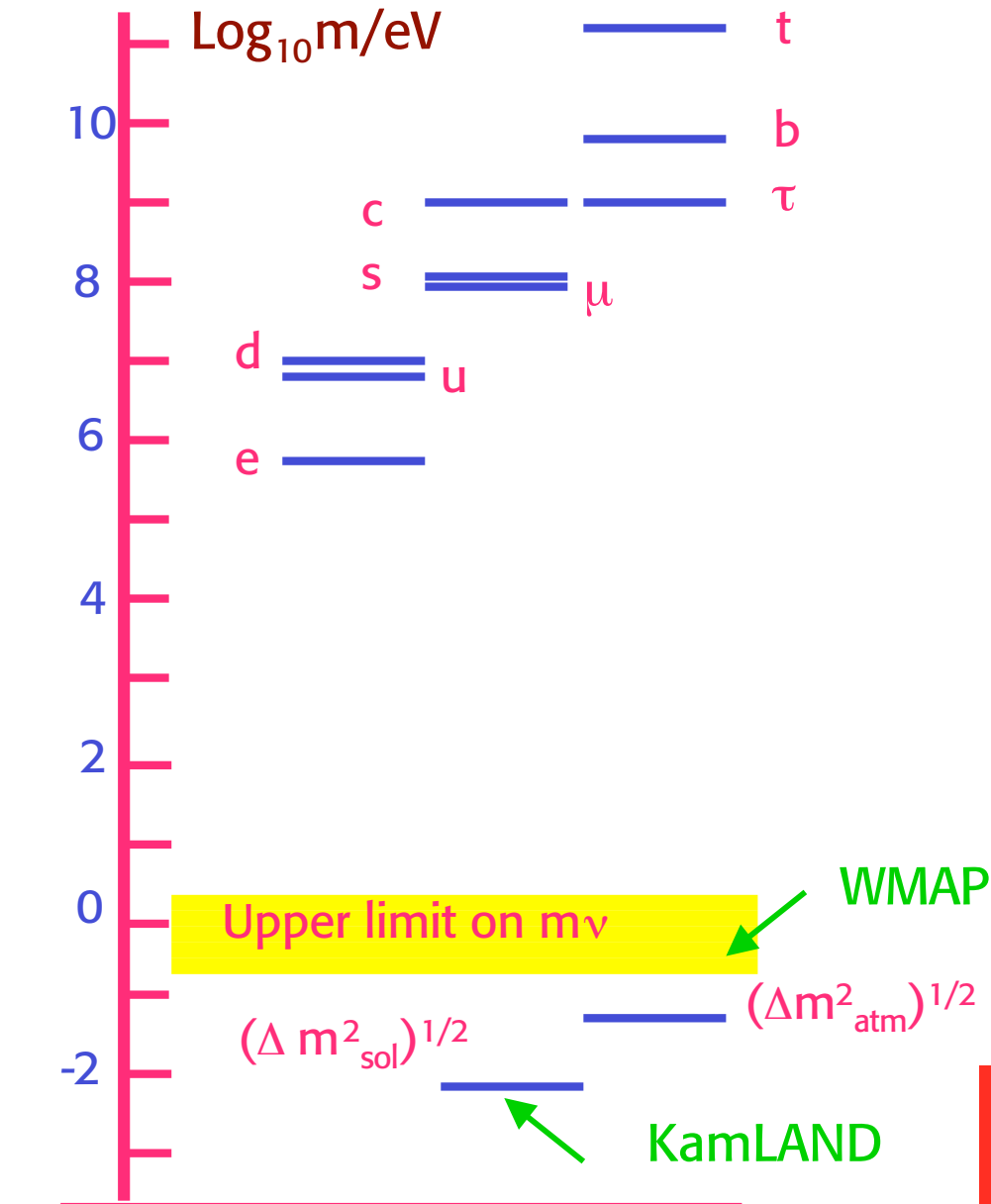
• **Coupling unification:** Precise matching of gauge couplings at  $M_{\text{GUT}}$  fails in SM and is well compatible in SUSY

Non SUSY GUT's  
 $\alpha_s(m_Z)=0.073\pm 0.002$

SUSY GUT's  
 $\alpha_s(m_Z)=0.130\pm 0.010$

Langacker, Polonski  
Dominant error:  
thresholds near  $M_{\text{GUT}}$

While GUT's and SUSY very well match,  
(best phenomenological hint for SUSY!)  
in technicolor, large extra dimensions,  
little higgs etc., there is no ground for GUT's



G. Altarelli

Neutrino masses are really special!

$m_t / (\Delta m^2_{atm})^{1/2} \sim 10^{12}$

Massless  $\nu$ 's?

- no  $\nu_R$
- L conserved

Small  $\nu$  masses?

- $\nu_R$  very heavy
- L not conserved

Neutrino masses point to  $M_{GUT}$ , well fit into the SUSY picture and in GUT's

A very natural and appealing explanation:

$\nu$ 's are nearly massless because they are Majorana particles and get masses through L non conserving interactions suppressed by a large scale  $M \sim M_{\text{GUT}}$

$$m_\nu \sim \frac{m^2}{M}$$

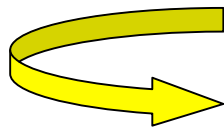
$$m \sim m_t \sim v \sim 200 \text{ GeV}$$

M: scale of L non cons.

Note:

$$m_\nu \sim (\Delta m_{\text{atm}}^2)^{1/2} \sim 0.05 \text{ eV}$$

$$m \sim v \sim 200 \text{ GeV}$$



$$M \sim 10^{15} \text{ GeV}$$

Neutrino masses are a probe of physics at  $M_{\text{GUT}}$  !

At the end of the XIX century J. J. Thompson proved the necessity of new physics (beyond em and gravity) proving that the energy from the sun and the stars cannot be obtained from chemistry

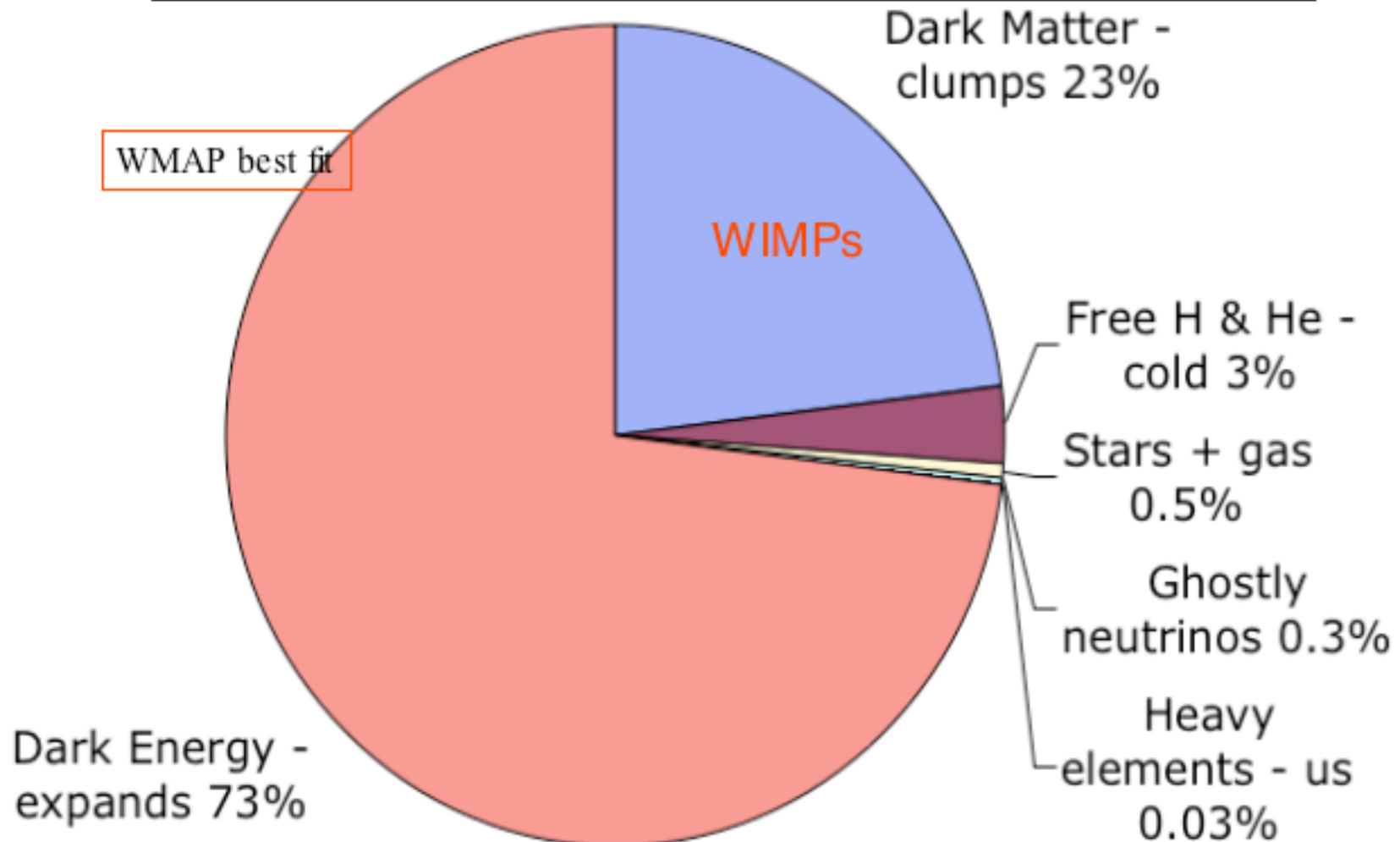
Today the clearest evidence for new physics comes from dark matter and dark energy

[More and more unity of particle physics and cosmology]

Dark matter could be accessible to present particle physics: a most important mission

G. Altarelli

# Composition of the Cosmos



Binetry

## Dark Matter

WMAP

Most of the Universe is not made up of atoms:  $\Omega_{\text{tot}} \sim 1$ ,  $\Omega_b \sim 0.044$ ,  $\Omega_m \sim 0.27$   
Most is Dark Matter and Dark Energy

Most Dark Matter is Cold (non relativistic at freeze out)

Significant Hot Dark matter is disfavoured

Neutrinos are not much cosmo-relevant:  $\Omega_\nu < 0.015$  (WMAP)

SUSY has excellent DM candidates: Neutralinos ( $\rightarrow$  LHC)

Also Axions are still viable

(in a mass window around  $m \sim 10^{-4}$  eV and  $f_a \sim 10^{11}$  GeV  
but these values are simply a-posteriori)

Identification of Dark Matter is a task of enormous importance for particle physics and cosmology

LHC?



LHC has good chances because it can reach any kind of WIMP:

WIMP: weakly interacting particle with  $m \sim 10^1\text{-}10^3$  GeV

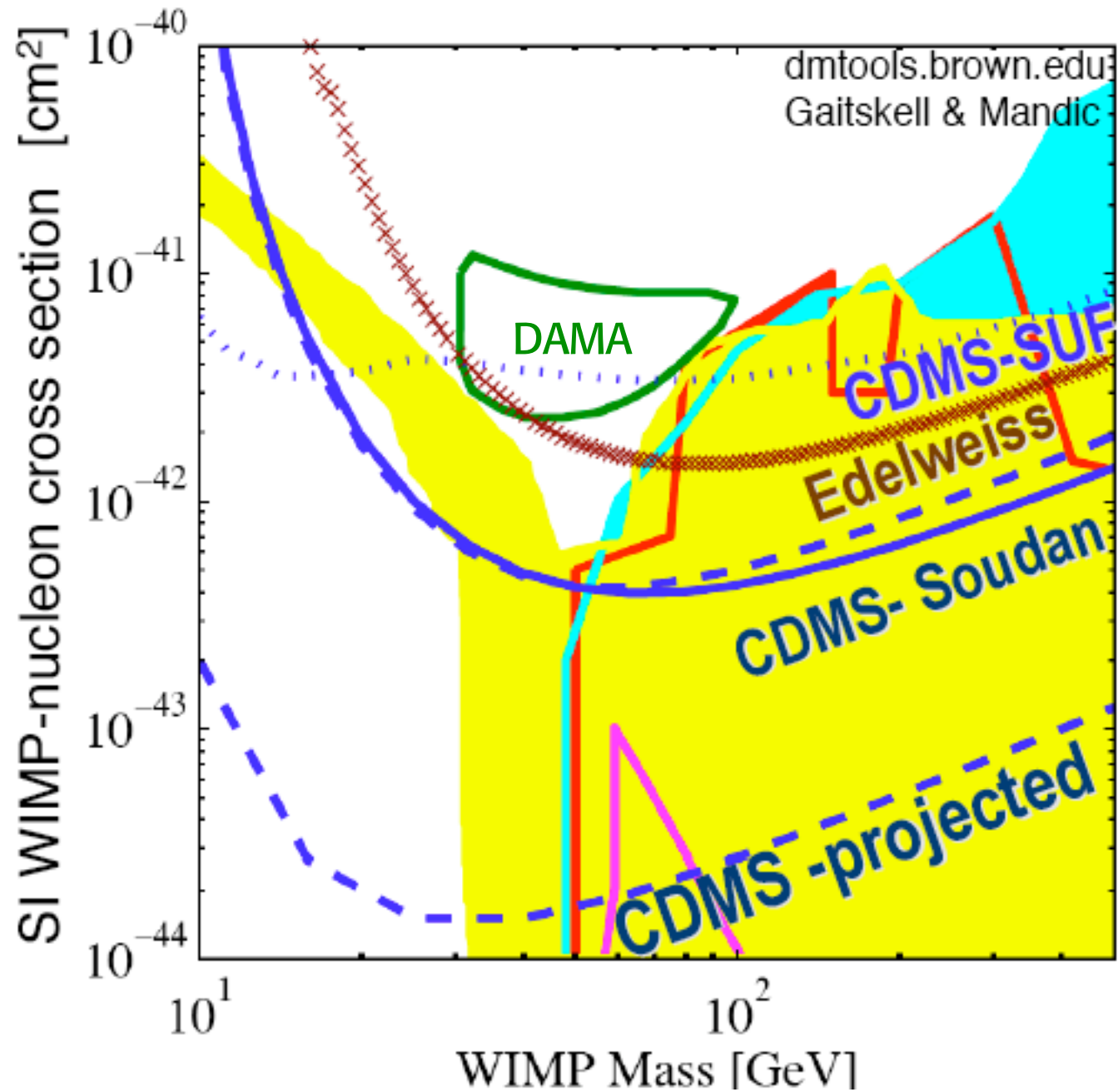
For WIMP's in thermal equilibrium after inflation the density is:

$$\Omega_\chi h^2 \simeq \text{const.} \cdot \frac{T_0^3}{M_{\text{Pl}}^3 \langle \sigma_A v \rangle} \simeq \frac{0.1 \text{ pb} \cdot c}{\langle \sigma_A v \rangle}$$

can work for typical weak cross-sections!!!

This "coincidence" is a good indication in favour of a WIMP explanation of Dark Matter

# Search for neutralinos

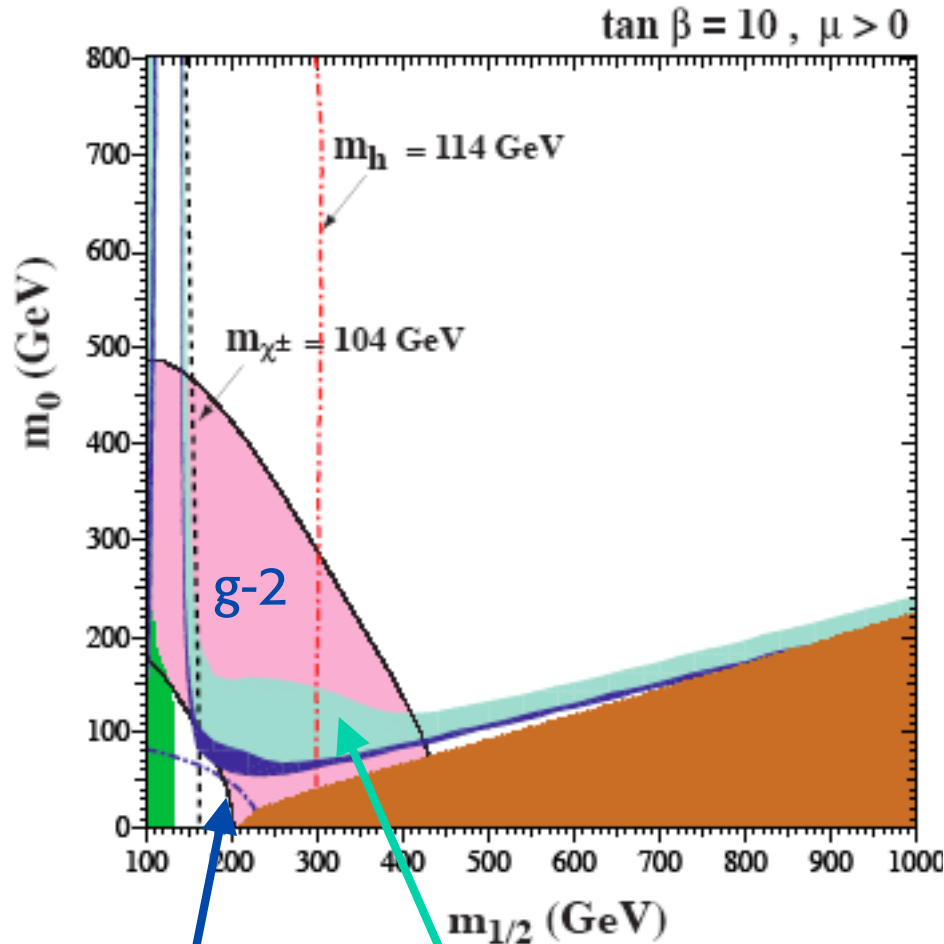


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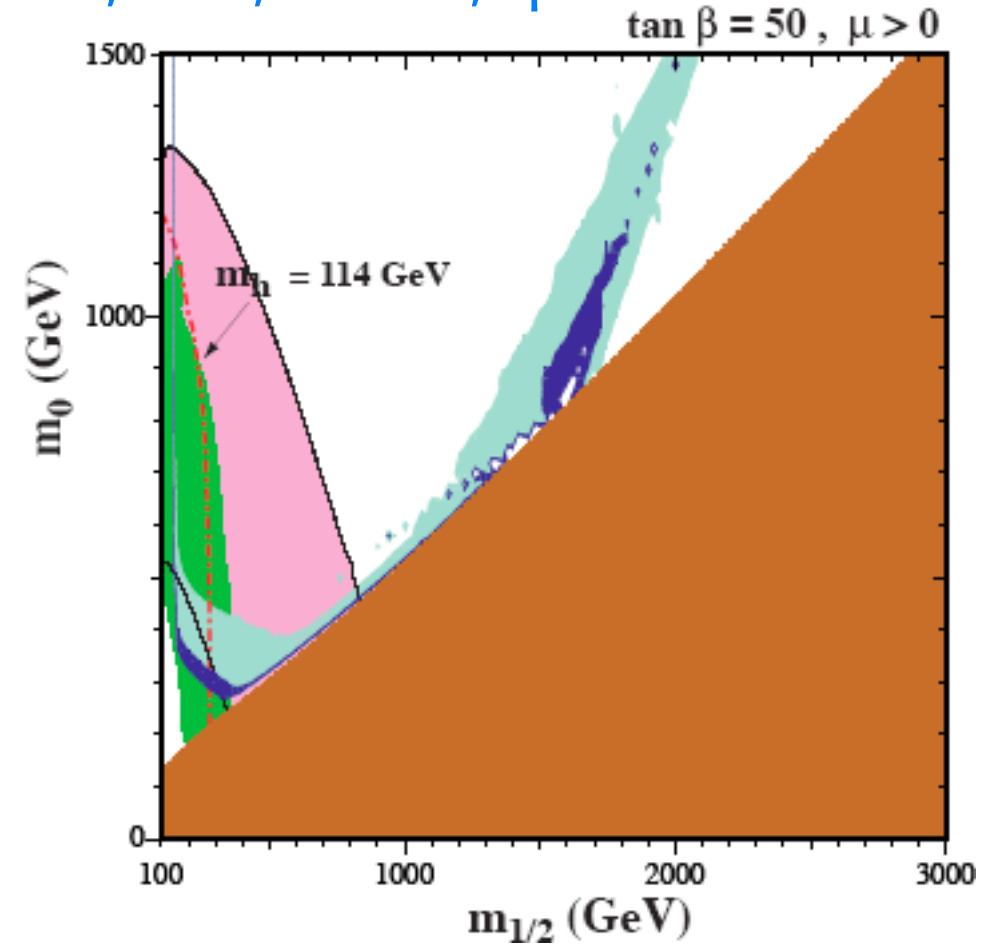
# SUSY Dark Matter: we hope it is the neutralino

Ellis, Olive, Santoso, Spanos

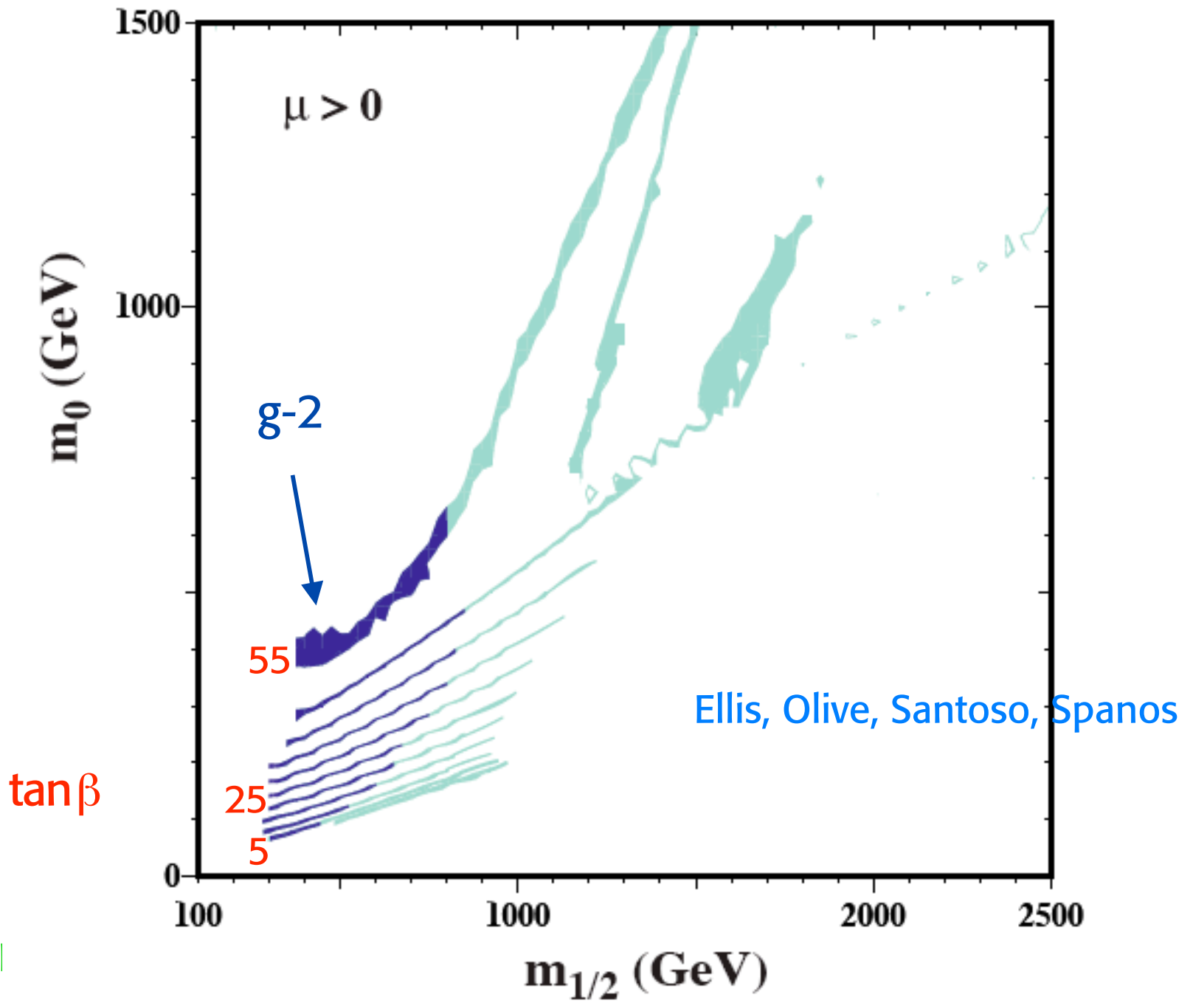


WMAP  
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$0.1 < \Omega h^2 < 0.3$



This is for the CMSSM  
With less constraints more space



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Neutrino masses point to  $M_{\text{GUT}}$ ,  
well fit into the SUSY-GUT's picture:



indeed add considerable support to  
this idea.

Technicolor, Little Higgs, Extra dim.....:  
nearby cut-off. Problem of suppressing

$$O_5 = v_L \frac{T \lambda}{M} v_L^{HH}$$

Another big plus of neutrinos is the elegant  
picture of baryogenesis thru leptogenesis  
(after LEP has disfavoured BG at the weak scale)

# Baryogenesis

A most attractive possibility:

## BG via Leptogenesis near the GUT scale

$T \sim 10^{12 \pm 3}$  GeV (after inflation)

Buchmuller, Yanagida,  
Plumacher, Ellis, Lola,  
Giudice et al, Fujii et al  
.....

Only survives if  $\Delta(B-L)$  is not zero  
(otherwise is washed out at  $T_{ew}$  by instantons)

Main candidate: decay of lightest  $\nu_R$  ( $M \sim 10^{12}$  GeV)

L non conserv. in  $\nu_R$  out-of-equilibrium decay:

B-L excess survives at  $T_{ew}$  and gives the obs. B asymmetry.

Quantitative studies confirm that the range of  $m_i$  from  
 $\nu$  oscill's is compatible with BG via (thermal) LG

In particular the bound  
was derived for hierarchy

$$m_i < 10^{-1} \text{ eV}$$

Can be relaxed for degenerate neutrinos  
So fully compatible with oscill'n data!!

Buchmuller, Di Bari, Plumacher;  
Giudice et al; Pilaftsis et al;  
Hambye et al

The scale of the cosmological constant is a big mystery.

$\Omega_\Lambda \sim 0.65$   $\longrightarrow$   $\rho_\Lambda \sim (2 \cdot 10^{-3} \text{ eV})^4 \sim (0.1 \text{ mm})^{-4}$

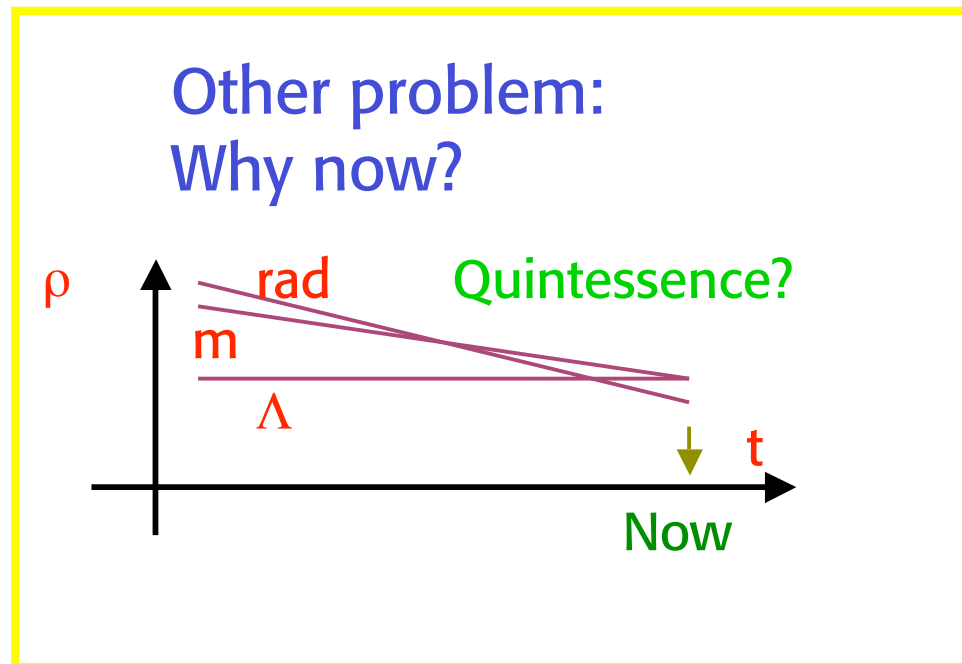
In Quantum Field Theory:  $\rho_\Lambda \sim (\Lambda_{\text{cutoff}})^4$   $\longrightarrow$  Similar to  $m_\nu$ !?

If  $\Lambda_{\text{cutoff}} \sim M_{\text{Pl}}$   $\longrightarrow$   $\rho_\Lambda \sim 10^{123} \rho_{\text{obs}}$

Exact SUSY would solve the problem:  $\rho_\Lambda = 0$

But SUSY is broken:  $\rho_\Lambda \sim (\Lambda_{\text{SUSY}})^4 \sim 10^{59} \rho_{\text{obs}}$

It is interesting that the correct order is  $(\rho_\Lambda)^{1/4} \sim (\Lambda_{\text{EW}})^2 / M_{\text{Pl}}$



The scale of vacuum energy poses a large naturalness problem!

So far no clear way out:

- A modification of gravity at 0.1 mm? (large extra dim.)
- Leak of vac. energy to other universes (wormholes)?

- Anthropic principle: just right for galaxy formation  
(Weinberg)

Perhaps naturalness irrelevant also for Higgs: Arkani-Hamed, Dimopoulos; Giudice, Romanino '04

Split SUSY: a fine tuned light Higgs + light gauginos and higgsinos. all other s-partners heavy preserves coupling unification and dark matter

Or simply a two-scale non-SUSY GUT with axions as DM  
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**But:** Lack of SUSY signals at LEP + lower limit on  $m_H$  problems for minimal SUSY

$m_{\text{stop}}$  large tends to clash with  $\delta m_h^2 \sim m_{\text{stop}}^2$

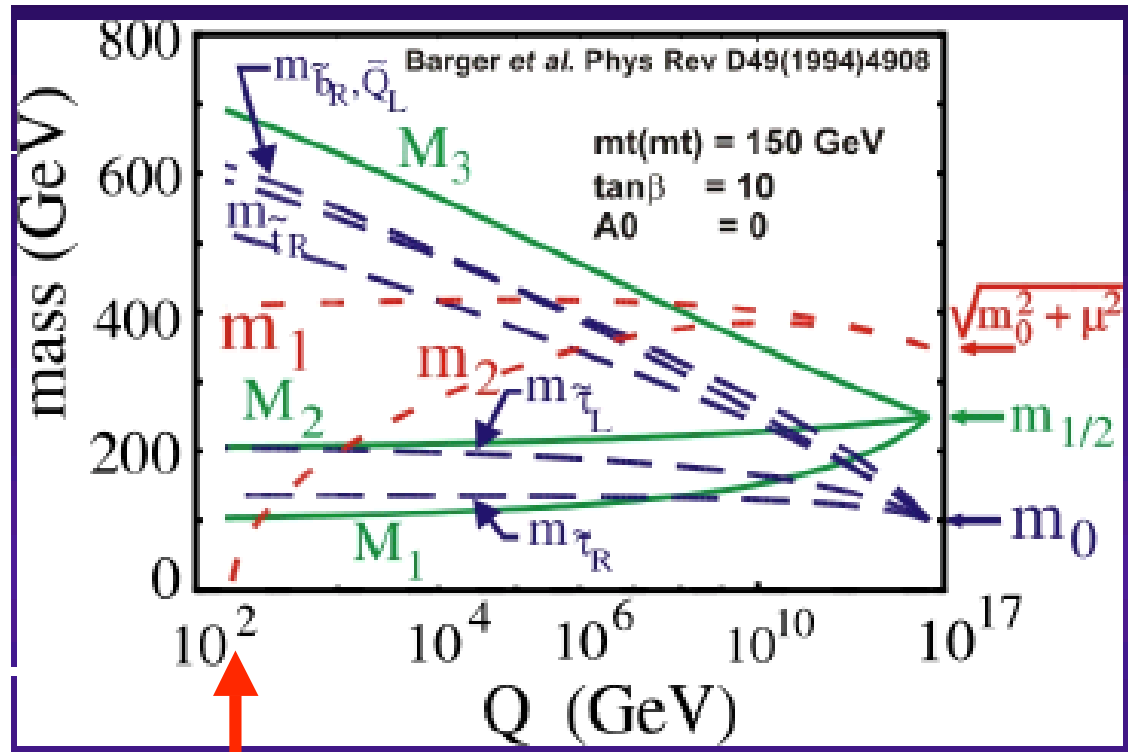
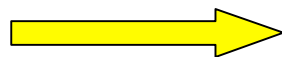
• In MSSM: 
$$m_h^2 \approx m_Z^2 \cos^2 2\beta + \frac{3\alpha_w m_t^4}{4\pi m_W^2 \sin^2 \beta} \ln \frac{\tilde{m}_t^4}{m_t^4} < \sim 130 \text{ GeV}$$

So  $m_H > 114 \text{ GeV}$  considerably reduces available parameter space.

• In SUSY EW symm. breaking is induced by  $H_u$  running

Exact location implies constraints

G. Altarelli



$m_Z$  can be expressed in terms of SUSY parameters

For example, assuming universal masses at  $M_{\text{GUT}}$  for scalars and for gauginos

$$m_Z^2 \approx c_{1/2} m_{1/2}^2 + c_0 m_0^2 + c_t A_t^2 + c_\mu \mu^2 \quad c_a = c_a(m_t, \alpha_i, \dots)$$

Clearly if  $m_{1/2}, m_0, \dots \gg m_Z$ : **Fine tuning!**

LEP results (e.g.  $m_{\chi^+} > \sim 100 \text{ GeV}$ ) exclude gaugino universality if no FT by  $> \sim 20$  times is allowed

Without gaugino univ. the constraint only remains on  $m_{\text{gluino}}$  and is not incompatible

$$m_Z^2 \approx 0.7 m_{\text{gluino}}^2 + \dots$$

[Exp. :  $m_{\text{gluino}} > \sim 200 \text{ GeV}$ ]

Barbieri, Giudice; de Carlos, Casas; Barbieri, Strumia; Kane, King;  
Kane, Lykken, Nelson, Wang.....

G. Altarelli



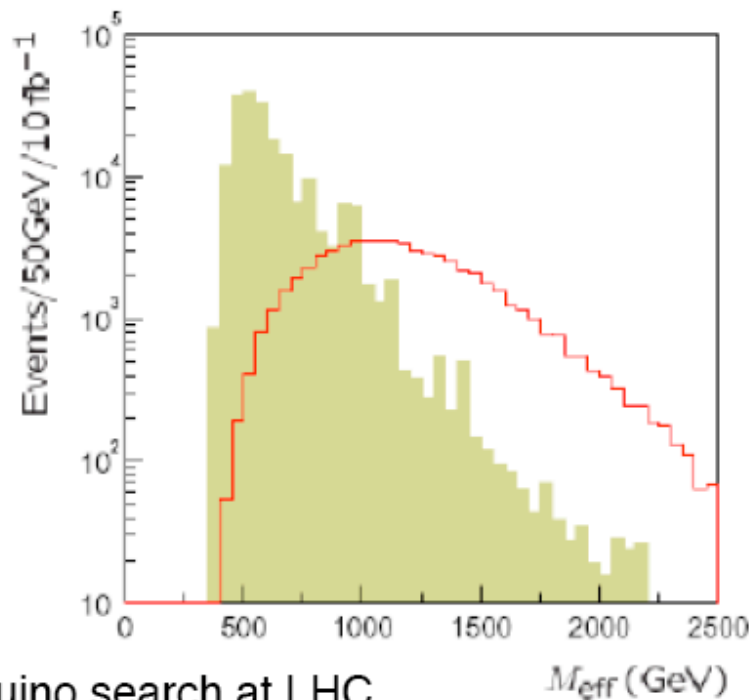
# Supersymmetry: the reactions to the “problem”

Barbieri, ICHEP'04

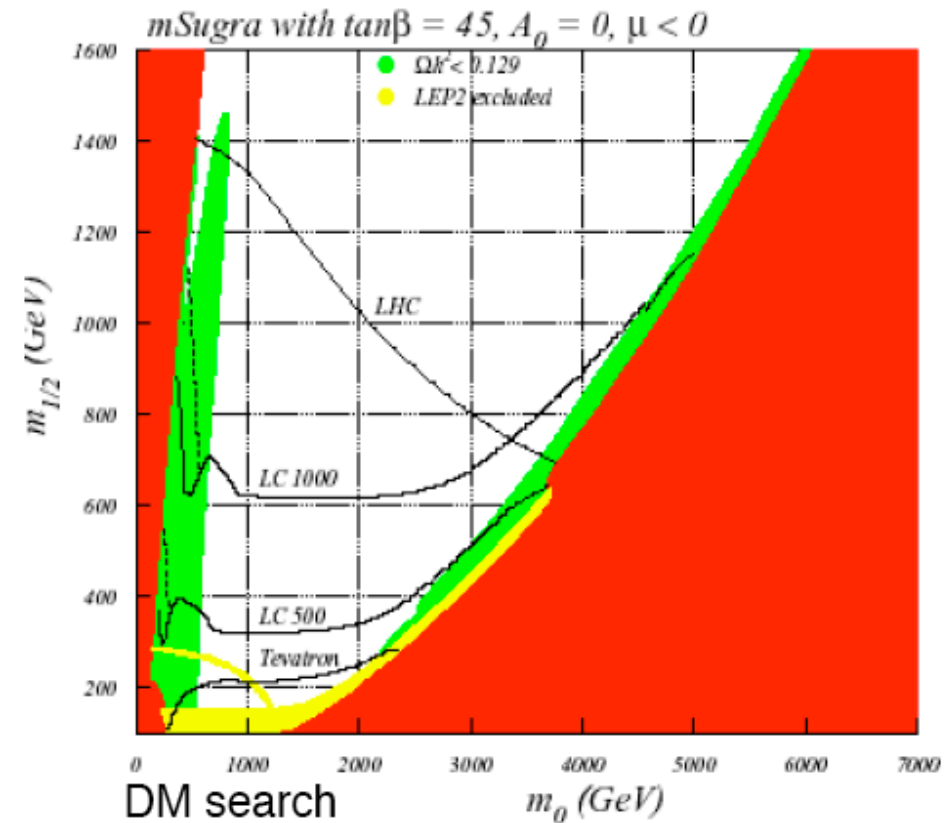
## I. Never mind a few % accidental tuning

LHC  $\oplus$  LC can systematically explore ~ all of the MSSM parameter space up to a per-mille tuning

$$m_h \leq 125 \div 130 \text{ GeV}$$



Gluino search at LHC  
ATLAS Coll



DM search  
Baer et al

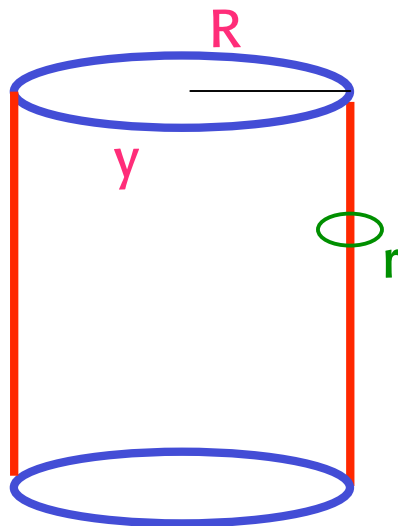
## Large Extra Dimensions

Solve the hierarchy problem by bringing gravity down from  $M_{\text{Pl}}$  to  $o(1\text{TeV})$

Arkani-Hamed, Dimopoulos/ Dvali+Antoniadis/ Randall,Sundrum.....

Inspired by string theory, one assumes:

- Large compactified extra dimensions
- SM fields are on a brane
- Gravity propagates in the whole bulk



$y$ : extra dimension  
 $R$ : compact'n radius

$y=0$  "our" brane (possibly with thickness  $r$ )

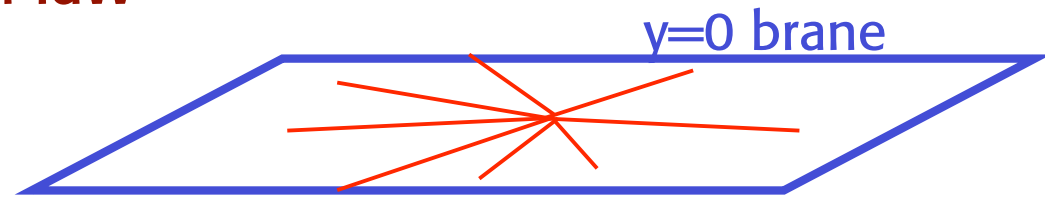
$G_N \sim 1/M_{\text{Pl}}^2$ :  
Newton const.  
 $M_{\text{Pl}}$  large as  
 $G_N$  weak

The idea is that gravity appears weak as a lot of lines of force escape in extra dimensions

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$r \gg R$ : ordinary Newton law

$$F \sim \frac{G_N}{r^2} \sim \frac{1}{M_{Pl}^2 r^2}$$

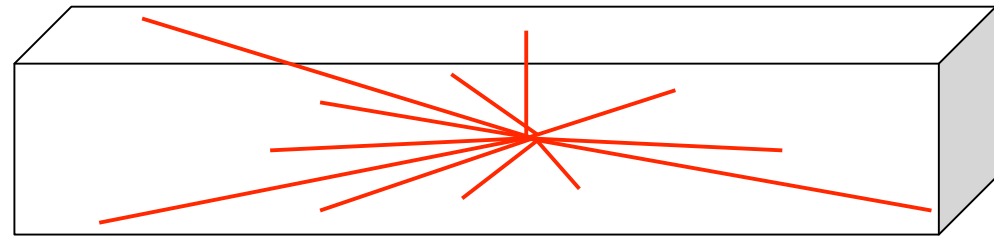


$r \ll R$ : lines in all dimensions

Gauss in  $d$  dim:

$$r^{d-2} \rho \sim m$$

$$F \sim \frac{1}{m^2 (mr)^{d-4} \cdot r^2}$$



By matching at  $r=R$

$$\left(\frac{M_{Pl}}{m}\right)^2 = (Rm)^{d-4}$$



For  $m \sim 1$  TeV, ( $d-4 = n$ )

$n = 1$   $R \sim 10^{15}$  cm (excluded)

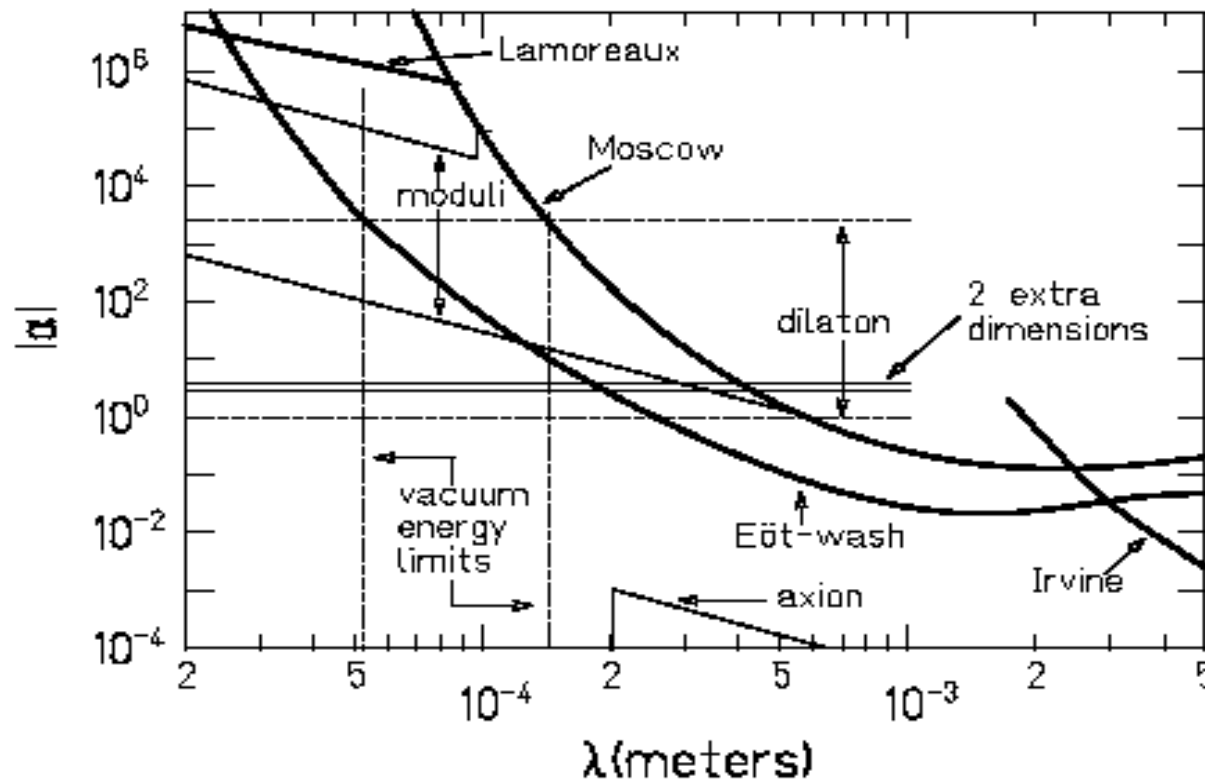
$n = 2$   $R \sim 1$  mm (close to limits)

$n = 4$   $R \sim 10^{-9}$  cm

...

## Limits on deviations from Newton law

$$V(r) = -G \frac{m_1 m_2}{r} (1 + \alpha e^{-r/\lambda})$$



Hoyle et al,  
PRL 86,1418,2001

FIG. 4. 95% confidence upper limits on  $1/r^2$ -law violating interactions of the form given by Eq. (2). The region excluded by previous work [2,3,20] lies above the heavy lines labeled Irvine, Moscow and Lamoreaux, respectively. The data in Fig. 3 imply the constraint shown by the heavy line labeled Eöt-wash. Constraints from previous experiments and the theoretical predictions are adapted from Ref. [8], except for the dilaton prediction which is from Ref. [14].

Generic feature:  
compact dim.

→ Kaluza-Klein (KK) modes



$$p = n/R \quad m^2 = n^2/R^2$$

(quantization in a box)

Many possibilities:

perhaps the most promising

G. Altarelli

• SM fields on a brane

The brane can itself have a thickness  $r$ :

$$1/r > \sim 1 \text{ TeV} \quad \rightarrow \quad r < \sim 10^{-17} \text{ cm}$$

→ KK recurrences of SM fields:  $W_n, Z_n$  etc

cfr: • Gravity on bulk

$$1/R > \sim 10^{-3} \text{ eV} \quad \rightarrow \quad R < \sim 0.1 \text{ mm}$$

• Factorized metric:

$$ds^2 = \eta_{\mu\nu} dx^\mu dx^\nu + h_{ij}(y) dy^i dy^j$$

• Warped metric:

Randall-Sundrum (R-S)

$$ds^2 = e^{-2mR|\varphi|} \eta_{\mu\nu} dx^\mu dx^\nu - R^2 \varphi^2$$



$$m = M_{\text{Pl}} \exp(-2mR\pi) \quad \rightarrow \quad Rm \sim 10$$

- Large Extra Dimensions is a very exciting scenario.
- However, by itself it is difficult to see how it can solve the main problems (hierarchy, the LEP Paradox)

\* Why  $(Rm)$  not  $O(1)$ ?

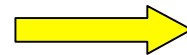
R-S better in this respect

$$\left(\frac{M_{Pl}}{m}\right)^2 = (Rm)^{d-4}$$

$$m = M_{Pl} \exp(-2mR\pi)$$

\*  $\Lambda \sim 1/R$  must be small ( $m_H$  light)

\* But precision tests put very strong lower limits on  $\Lambda$  (several TeV)

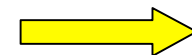


In fact in typical models of this class there is no mechanism to sufficiently quench the corrections

• But could be part of the truth!

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• Interesting directions explored

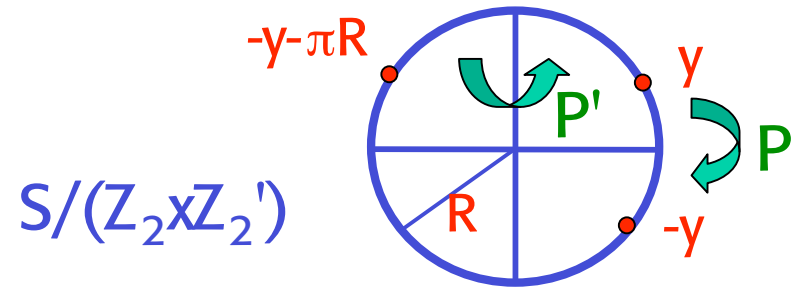


# Symmetry breaking by orbifolding

For  $1/R \sim M_{\text{GUT}}$

GUT's in ED: very appealing  
 SU(5), SO(10) in 5 or 6 dimensions

Kawamura/GA, Feruglio/ Hall, Nomura;  
 Hebecker, March-Russell;  
 Hall, March-Russell, Okui, Smith  
 Asaka, Buchmuller, Covi  
 ....



$$Z_2 \rightarrow P: y \leftrightarrow -y$$

$$Z_2' \rightarrow P': y' \leftrightarrow -y'$$

$$y' = y + \pi R/2$$

$$\text{or } y \leftrightarrow -y - \pi R$$

- No baroque Higgs system
- Natural doublet-triplet splitting
- Coupling unification can be maintained

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$$\phi_{++}(x_\mu, y) = \sqrt{\frac{2}{\pi R}} \cdot \sum_n \phi_{++}^{(2n)}(x_\mu) \cos \frac{2ny}{R}$$

$$\phi_{+-}(x_\mu, y) = \sqrt{\frac{2}{\pi R}} \cdot \sum_n \phi_{+-}^{(2n+1)}(x_\mu) \cos \frac{2n+1}{R} y$$

$$\phi_{-+}(x_\mu, y) = \sqrt{\frac{2}{\pi R}} \cdot \sum_n \phi_{-+}^{(2n+1)}(x_\mu) \sin \frac{2n+1}{R} y$$

$$\phi_{--}(x_\mu, y) = \sqrt{\frac{2}{\pi R}} \cdot \sum_n \phi_{--}^{(2n+2)}(x_\mu) \sin \frac{2n+2}{R} y$$

# Symmetry breaking at the weak scale

$$1/R \sim o(\text{TeV})$$

- SUSY Breaking**

Barbieri, Hall, Nomura.....Papucci, Marandella.

## 5D SUSY-SM compactified on $S/(Z_2-Z_2')$

- $Z$  breaks  $N=2$  SUSY,  $Z'$   $N=1$  SUSY (Scherk-Schwarz)

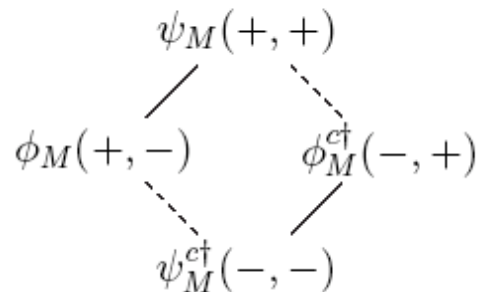
effective theory non-SUSY (SUSY recovered at  $d < R$ )

- Higgs boson mass in principle computable

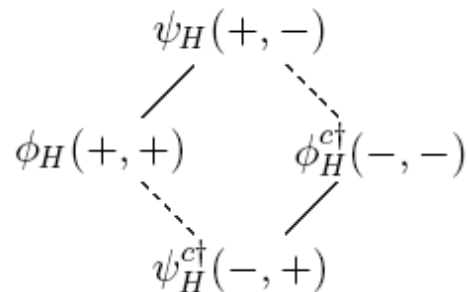
no invariant Higgs mass operator in 5-dim

rather insensitive to UV

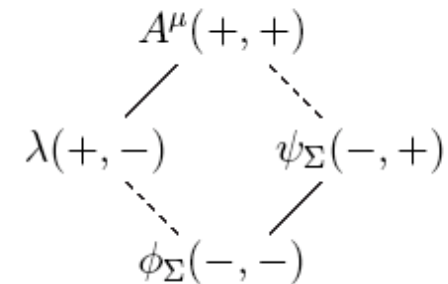
$$m_H \sim 110 - 125 \text{ GeV}$$



G. Altarelli matter



Higgs (only 1!)  
all are in the bulk

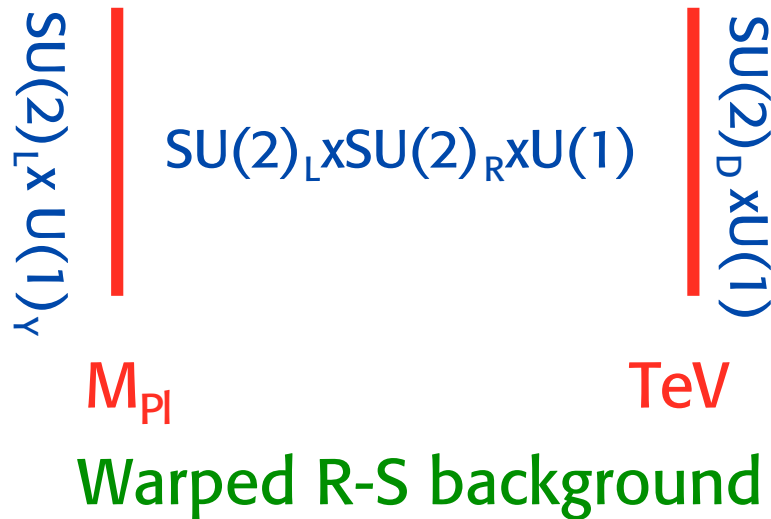


gauge



- **Gauge Symmetry Breaking (Higgsless theories)**

Csaki et al/Nomura/Davoudiasl et al/Barbieri, Pomarol, Rattazzi;....



Symmetries broken by Boundary Conditions (BC) on the branes →

Altogether only  $U(1)_Q$  unbroken

- Unitarity breaking (no Higgs) delayed by KK recurrences
- Dirac fermions on the bulk (L and R doublets). Only one chirality has a zero mode on the interval

A new way to look at walking technicolor by AdS/CFT correspondence

G. Altarelli But: serious problems with EW precision tests  
 e.g. Barbieri, Pomarol, Rattazzi, Strumia, Chivukula et al

# y-Boundary Conditions

## A scalar example

Action: 
$$S = \int dx \int dy \left[ \frac{1}{2} (\partial_M \phi)^2 - V(\phi) \right] + \int_{y=0, \pi R} dx \left[ \frac{1}{2} M^2 \phi^2 \right]$$

Varying the action: 
$$\delta S = \int dx \int dy \left[ \square \phi + \frac{\partial V}{\partial \phi} \right] \delta \phi + \int dx [(\partial_y \phi - M^2 \phi) \delta \phi]_0^{\pi R}$$

Thus, at  $y=0, \pi R$   $\phi_{0, \pi R} = cte \Rightarrow 0$  or  $[\partial_y \phi - M^2 \phi]_{0, \pi R} = 0$

Note:  $M^2 \rightarrow 0$   $[\partial_y \phi]_{0, \pi R} = 0$  Neumann  $\phi \sim \cos \frac{ny}{R}$

$M^2 \rightarrow \text{infinity}$   $\phi_{0, \pi R} = 0$  Dirichlet  $\phi \sim \sin \frac{ny}{R}$

Gauge theory:  $(A_\mu^a)_{0, \pi R} = 0$  or  $[\partial_y A_\mu^a - V^{ab} A_\mu^b]_{0, \pi R} = 0$

G. Altarelli  $V^{ab} = vt^a t^b v$  can arise from a Higgs H localised on the brane:  $D_M H = D^M H, D_M = \dots + t^a A_M^a, \langle H \rangle = v$

Suppose we want, at  $y=\pi R$ :

$$\partial_y A = VA$$

We set:  $A = A_0 \cos My$

Note. At  $y=0$ :  $\partial_y A = 0$

We find  $M$  (mass of boson  $A$ ):

$$-M \sin M\pi R = V \cos M\pi R$$

$$-M\pi R \sin M\pi R = V\pi R \cos M\pi R$$

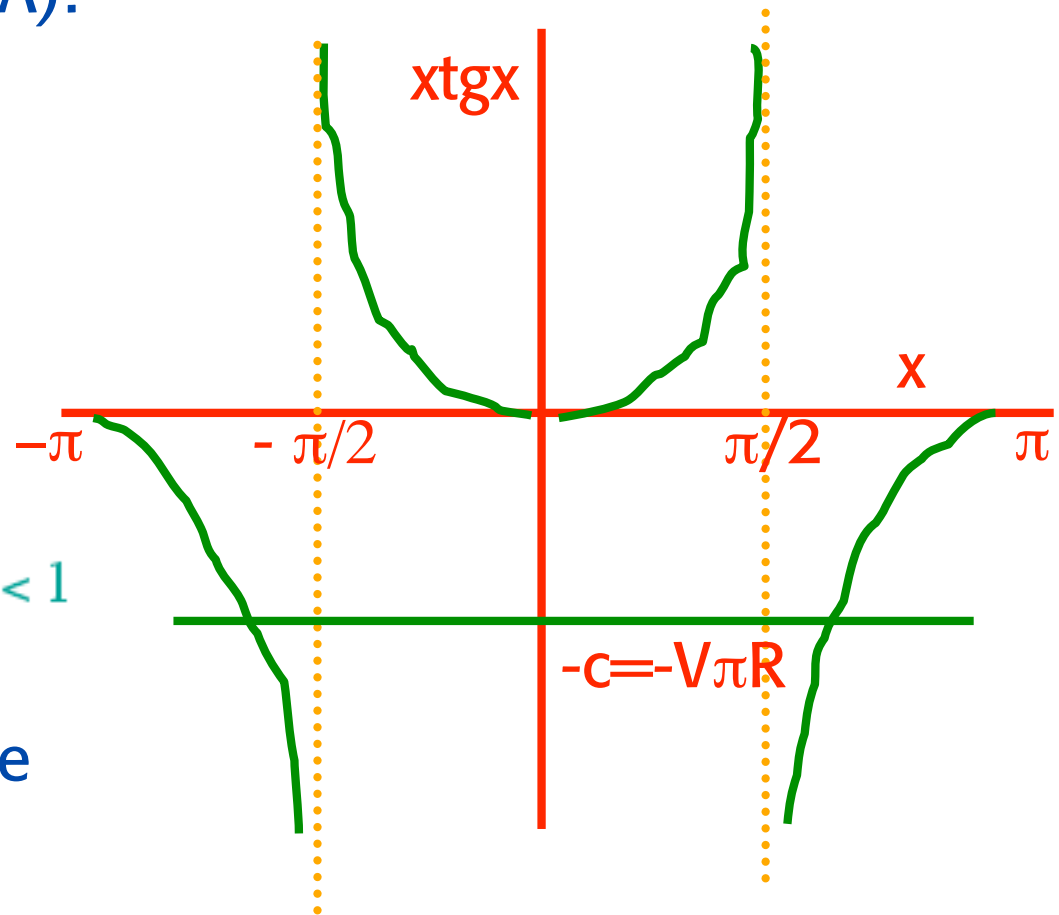


$$x \operatorname{tg} x = -c$$

$$\frac{\pi}{2} < |x| < \pi \quad \longrightarrow \quad \frac{1}{2} < |MR| < 1$$

Note that  $MR$  remains finite for  $V \rightarrow \infty$

G. Altarelli



Boundary conditions allow a general breaking pattern  
(for example, can lower the rank of the group)  
equivalent to have generic Higgses on the brane

Breaking by orbifolding is more rigid  
(the rank remains fixed)  
corresponds to Higgs in the adjoint ( $A_5$  the 5th  $A_M$ )

No realistic Higgsless model for EW symmetry breaking  
so far emerged

However be alerted of possible signals at the LHC:  
no Higgs but KK recurrences of  $W$ ,  $Z$  and additional  
gauge bosons

# Little Higgs Models

Georgi (moose)/Arkani-Hamed et al/Low, Skiba,  
Smith/Kaplan, Schmaltz/Chang,Wacker/Gregoire et al

$$G \supset [SU(2) \otimes U(1)]^2 \supset SU(2) \otimes U(1)$$

↑
↑
↑  
 global            gauged            SM

H is (pseudo)-Goldstone boson of G: takes mass only at 2-loops (needs breaking of 2 subgroups or 2 couplings)

cut off  $\Lambda$  ~10 TeV

$\Lambda^2$  divergences canceled by:

$\delta m^2_{H top}$	new coloured fermion $\chi$	}	~1 TeV
$\delta m^2_{H gauge}$	$W', Z', \gamma'$		
$\delta m^2_{H Higgs}$	new scalars		
	2 Higgs doublets		~0.2 TeV

E-W Precision Tests? Problems  
GUT's? But signatures at LHC clear

e.g.: enlarge  $SU(2)_{\text{weak}} \longrightarrow$  global  $SU(3)$

quark doublet  $\longrightarrow$  triplet

$$\begin{bmatrix} t_L \\ b_L \\ \chi_L \end{bmatrix}$$

$SU(3)$  broken spont.ly

$$\varphi = \exp i \frac{\begin{bmatrix} - & h \\ h^\dagger & - \end{bmatrix}}{f} \begin{bmatrix} 0 \\ 0 \\ f \end{bmatrix}$$

Yukawa coupling:

$$\lambda \begin{bmatrix} t_L^\dagger & b_L^\dagger & \chi_L^\dagger \end{bmatrix} \exp i \frac{\begin{bmatrix} - & h \\ h^\dagger & - \end{bmatrix}}{f} \begin{bmatrix} 0 \\ 0 \\ f \end{bmatrix} t_R + M \chi_L^\dagger \chi_R$$

expl.  $SU(3)$  breaking  $\swarrow$



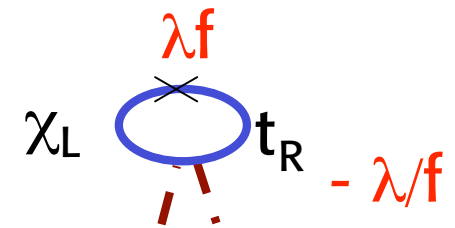
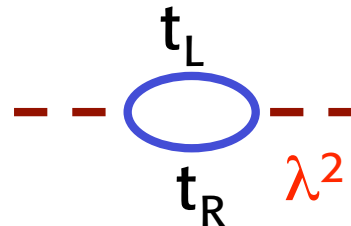
$$\lambda f \chi_L^\dagger t_R + i\lambda \begin{bmatrix} t_L^\dagger & b_L^\dagger \end{bmatrix} h t_R - \frac{\lambda}{2f} \chi_L^\dagger t_R h^\dagger h + \dots$$



top loop:

coeff.  $\Lambda^2$

G. Altarelli



# Little Higgs: Big Problems with Precision Tests

Hewett, Petriello, Rizzo/ Csaki et al/Casalbuoni, De Andrea, Oertel/  
Kilian, Reuter/

Even with vectorlike new fermions large corrections arise mainly from  $W'_i, Z'$  exchange.

[lack of custodial SU(2) symmetry]

A combination of LEP and Tevatron limits gives:

$$f > 4 \text{ TeV at } 95\% (\Lambda = 4\pi f)$$

Fine tuning  $> 100$  needed to get  $m_h \sim 200 \text{ GeV}$   
better if  $m_H$  heavier 

Presumably can be fixed by complicating the model

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## Back to 4D: the little Higgs models

Keep the essence of 5D, while avoiding its constraints by suitable (somewhat *ad hoc*) tricks

$$G_5 \simeq G_{gl} \text{ broken to } H_{gl} \quad G_{IR} \simeq H_{gl} \quad G_{UV} \simeq G_{gauge}$$

Problems: give the Higgs a quartic self-coupling and a top-Yukawa consistent with observations

(Too) many models:

The “littlest”  $f = \Lambda_{LH}$  The “simplest”

$$\text{Global} \quad SU(5) \xrightarrow{f} SO(5) \quad (SU(3)XU(1))^2 \xrightarrow{f} (SU(2)XU(1))^2$$

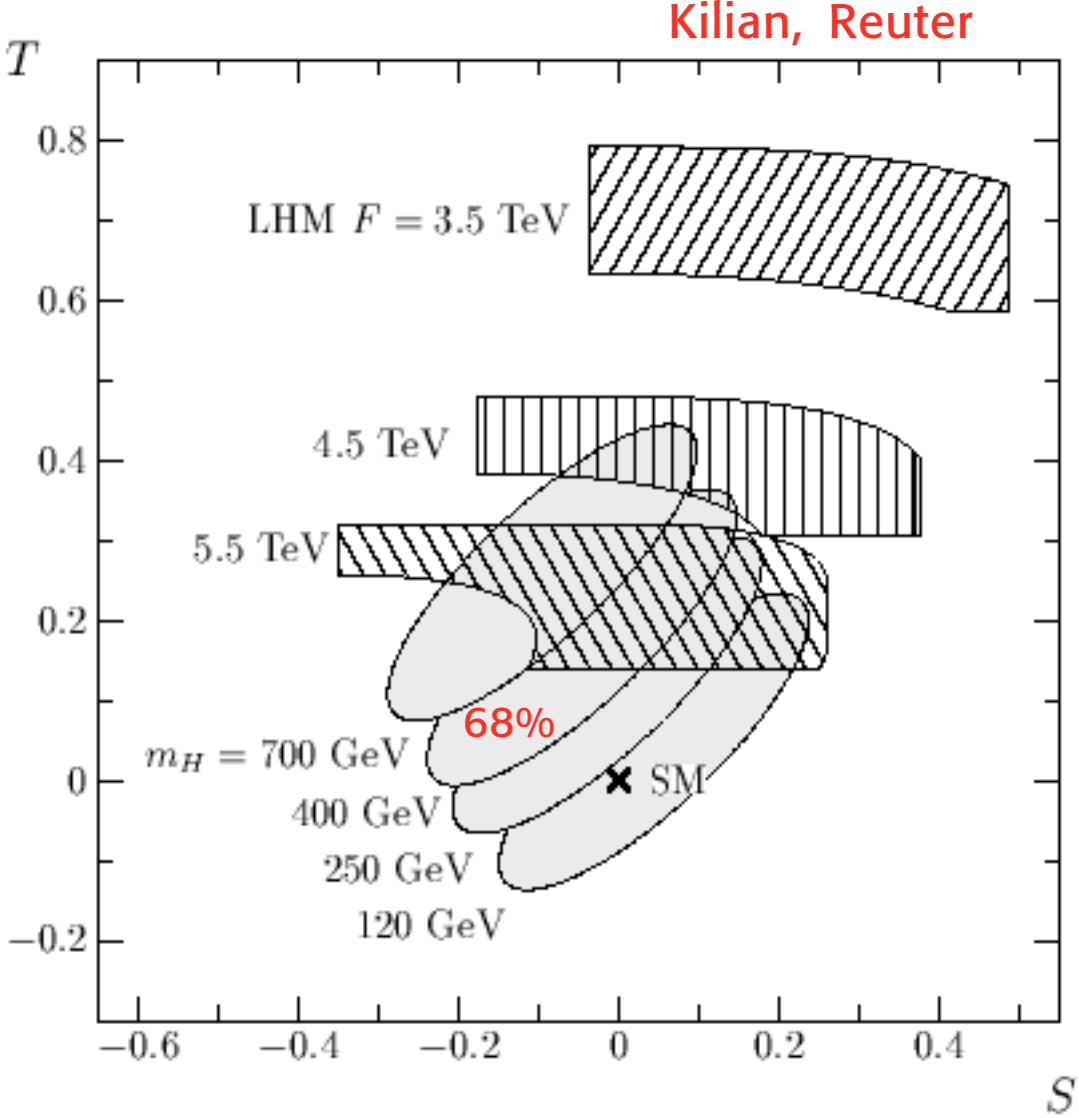
$$\text{Gauge} \quad (SU(2)XU(1))^2 \implies SU(2)XU(1) \quad SU(3)XU(1) \implies SU(2)XU(1)$$

Arkani-Hamed et al

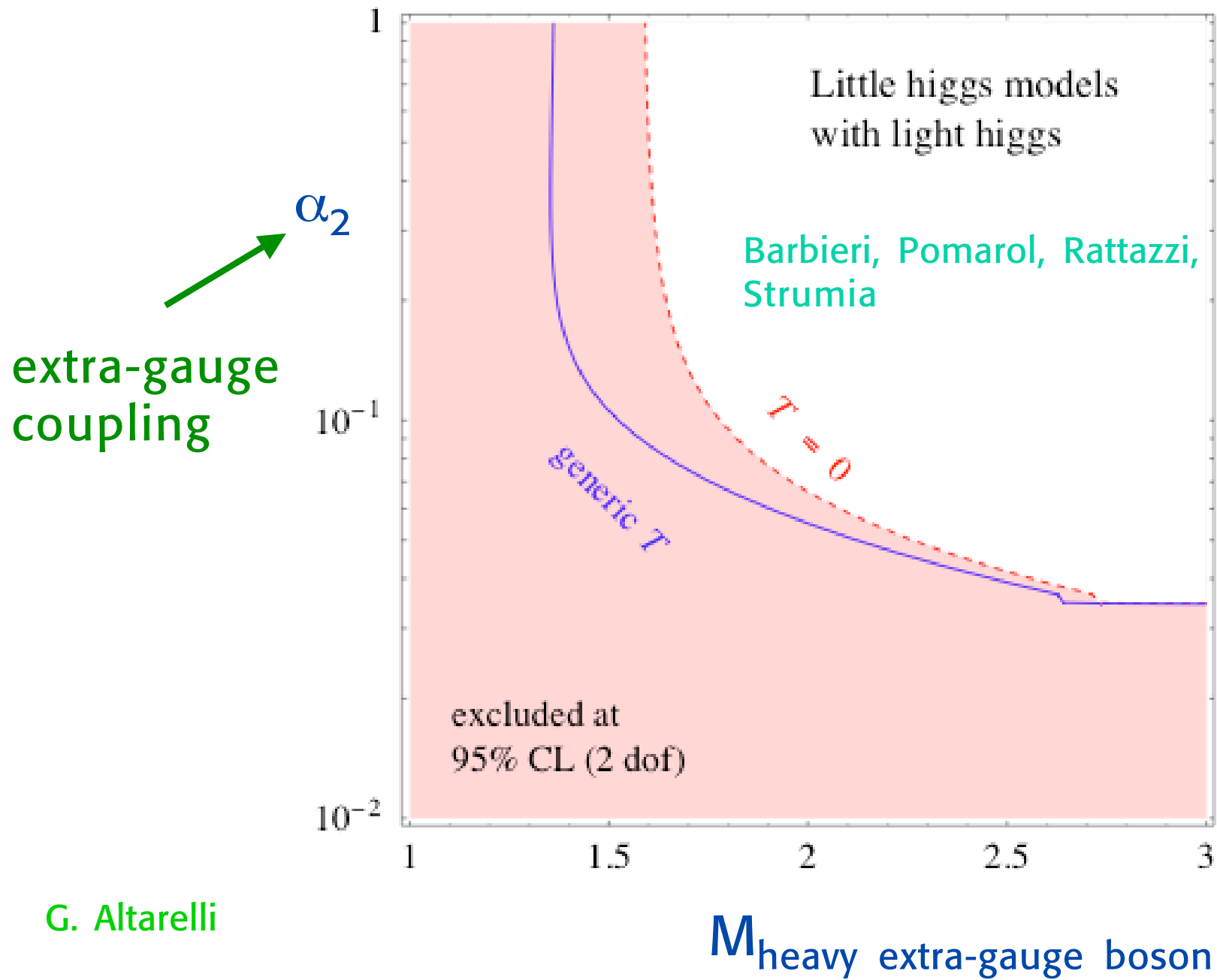
Kaplan, Schmaltz



For a light Higgs  $F$  ( $=f$ ) must be large.  
Better if  $m_H$  increases



G. Altarelli



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## Summarizing

- SUSY remains the Standard Way beyond the SM
- What is unique of SUSY is that it works up to GUT's .  
GUT's are part of our culture!  
Coupling unification, neutrino masses, dark matter, ....  
give important support to SUSY
- It is true that the train of SUSY is already a bit late  
(this is why there is a revival of alternative model building)
- No complete, realistic alternative so far developed  
(not an argument! But...)
- Extra dim.s is a complex, rich, attractive, exciting  
possibility.
- Little Higgs models look as just a postponement  
(both interesting to pursue)