

# Angular dependence of Recombination ?

## Reminder/Status

In Liquid Argon Ionization chambers the collected charge  $Q$  is different from the produced charge  $Q_0$  due to Electron Recombination :

$$Q = \mathcal{R}Q_0 ; \mathcal{R} \leq 1$$

$\mathcal{R}$  is function of the electric field  $\mathcal{E}$  and of the particle stopping power  $\frac{dE}{dx}$ . The **Birks** law (from columnar theory) usually reproduces data

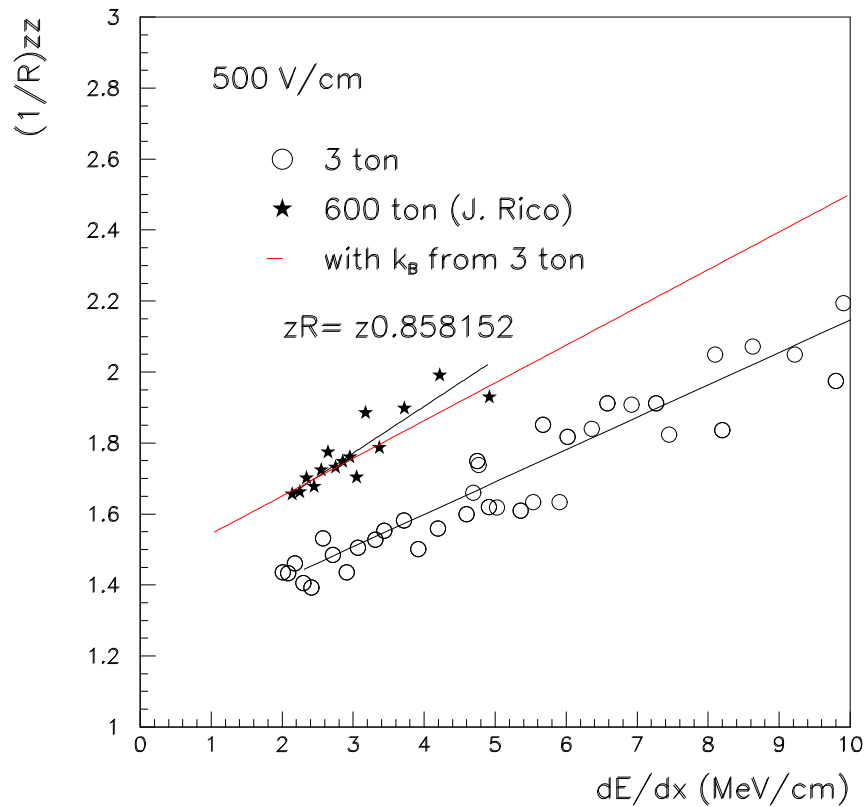
$$Q(\mathcal{E}) = \frac{Q_0}{1 + k/\mathcal{E}} \quad \text{or} \quad Q\left(\frac{dE}{dx}\right) = A \frac{Q_0}{1 + k_Q \frac{dE}{dx}}$$

$\searrow$   $k_Q = \frac{k}{\mathcal{E}}$   $\swarrow$

Other possibility: box model

$$Q(\mathcal{E}) = \frac{\log 1 + \xi}{\xi} ; \quad \xi \propto \frac{1}{E} \quad (1)$$

## ICARUS DataSets



ICARUS  $1/\mathcal{R}$  vs.  $\frac{dE}{dx}$

3 ton data :  $\mu, p$

300 t data :  $\mu$  (J. Rico)

$k$  values compatible

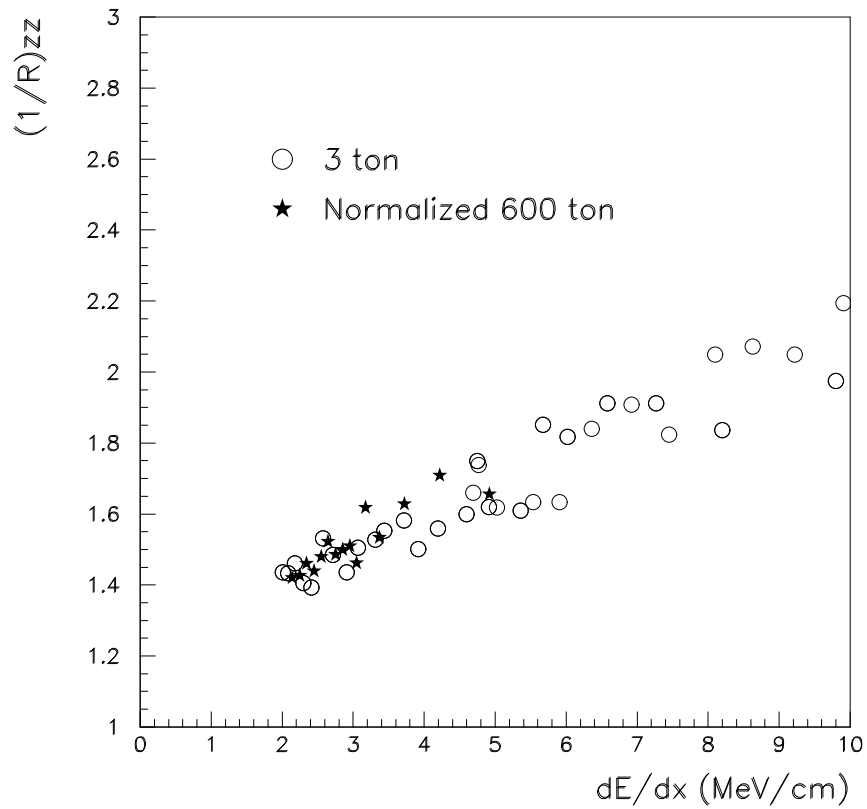
Different normalization

For simulations:

$k$  from 3ton

$A$  from 300 ton

## ICARUS DataSets



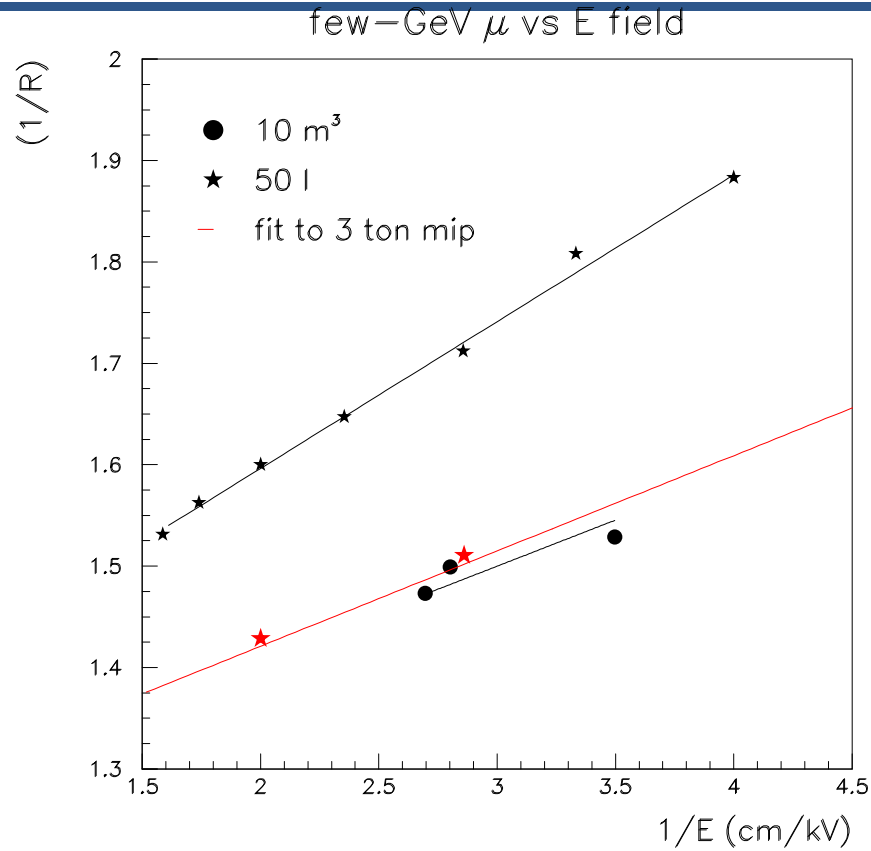
ICARUS  $1/\mathcal{R}$  vs.  $\frac{dE}{dx}$

3 ton data :  $\mu, p$

300 t data :  $\mu$  (J. Rico)

Constant Renormalisation

## ICARUS DataSets



ICARUS  $1/\mathcal{R}$  vs.  $\mathcal{E}$

*muons*

50 l (Silvia, Francesco)

10 m<sup>3</sup>, (Ornella)

3 t from fitted k

## Status

### For 600t simulations

We have now experimental slope and normalization.

MC can reproduce 600t data

### For recombination paper

Normalization to be understood

No hint from calibration tests

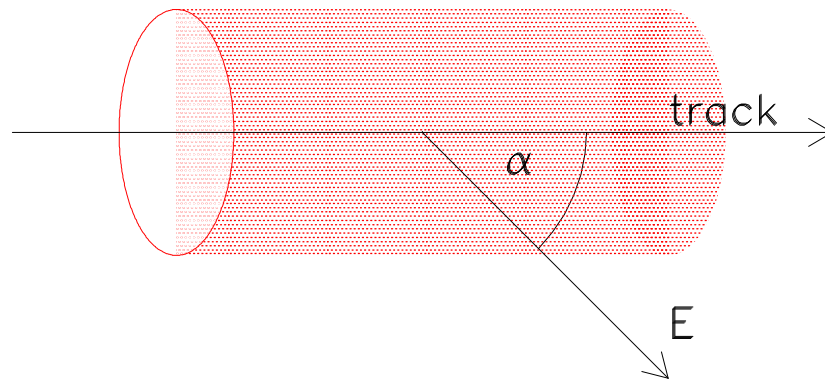
Test with  $\mu$  in 50l in program (soon)

Analysys of angular dependence- this meeting

## Angular dependence?

A dependence of recombination on the angle  $\alpha$  between  $\mathcal{E}$  and the track direction is foreseen in the columnar theory (Jaffè, Kramer):

$$\mathcal{E} \rightarrow \mathcal{E} \cdot \sin \alpha \text{ " for not too small } \alpha \text{ "}$$



What matters is the time spent inside the column

## Angular dependence in FLUKA

Given a track at an angle  $\alpha$  with the drift field

For each substep in each subtrack

find  $\beta$  angle between subtrack and  $\mathcal{E}$

redefine the Birks  $k$  as  $k / \sin \beta$

Small angle limit::?

First guess: limit from longitudinal path  $S$  needed to have

diffusion radius  $>$  radius of ionization column

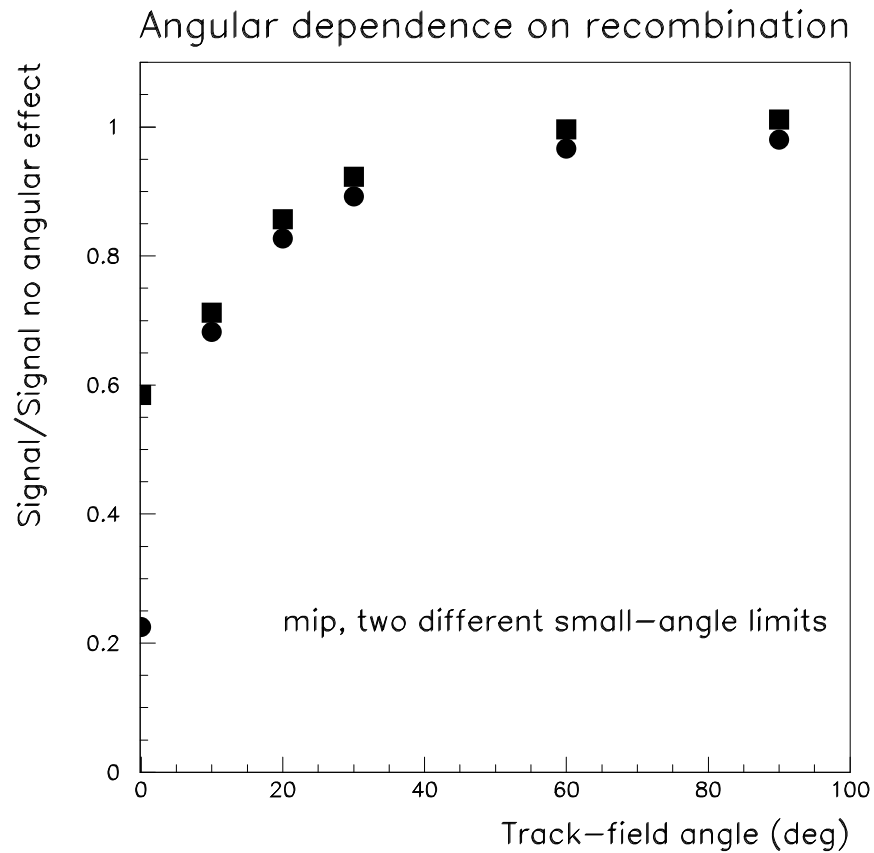
If  $D = 5 \text{ cm}^2/\text{s}$ , (3ton paper),  $v=1.5 \text{ mm}/\mu\text{s}$ ,  $r^2 = 4DS/v_{drift}$

$r/S = 0.1$  for  $r=100\text{nm}$  ,  $r/S = 0.01$  for  $r=10\text{nm}$

Ask also  $S <$  track length



## Angular dependence?



FLUKA recombination  
mip muon  
vs  $\alpha$  : muon track- $\mathcal{E}$  angle  
normalized to no angular  
dependence  
Birks  $k$  from ICARUS data  
→ 10 % at  $30^\circ$   
→ Uncertain at low  $\alpha$